



**Deutscher Wetterdienst**  
*Wetter und Klima aus einer Hand*



# Special Lecture on Assimilation of Radar Data

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1. Motivation
2. Basics on Radar meteorology
3. Radar measurement and its assimilation
  - Reflectivity
    - LHN
  - Radial Wind Component
    - VAD
    - Nudging
  - Polarisation
4. Brief introduction on Radar Forward Operator (for the LETKF era)





What have you learned already?

- Theoretical background on DA
  - To obtain a good analysis you need suitable measurements:  
Measuring of relevant parameter with a high resolution in space and time and a reasonable quality
- Satellite Observations:
  - Indirect measurement
  - reasonable resolution in space or time (normally not both together)
- Conventional Observations (Synops, Radio sondes):
  - direct measurement of relevant parameters
  - Sparse in space and/or time
- Further observation systems are available, but most of them will lack of high resolution in space (at least in one dimension) or time.



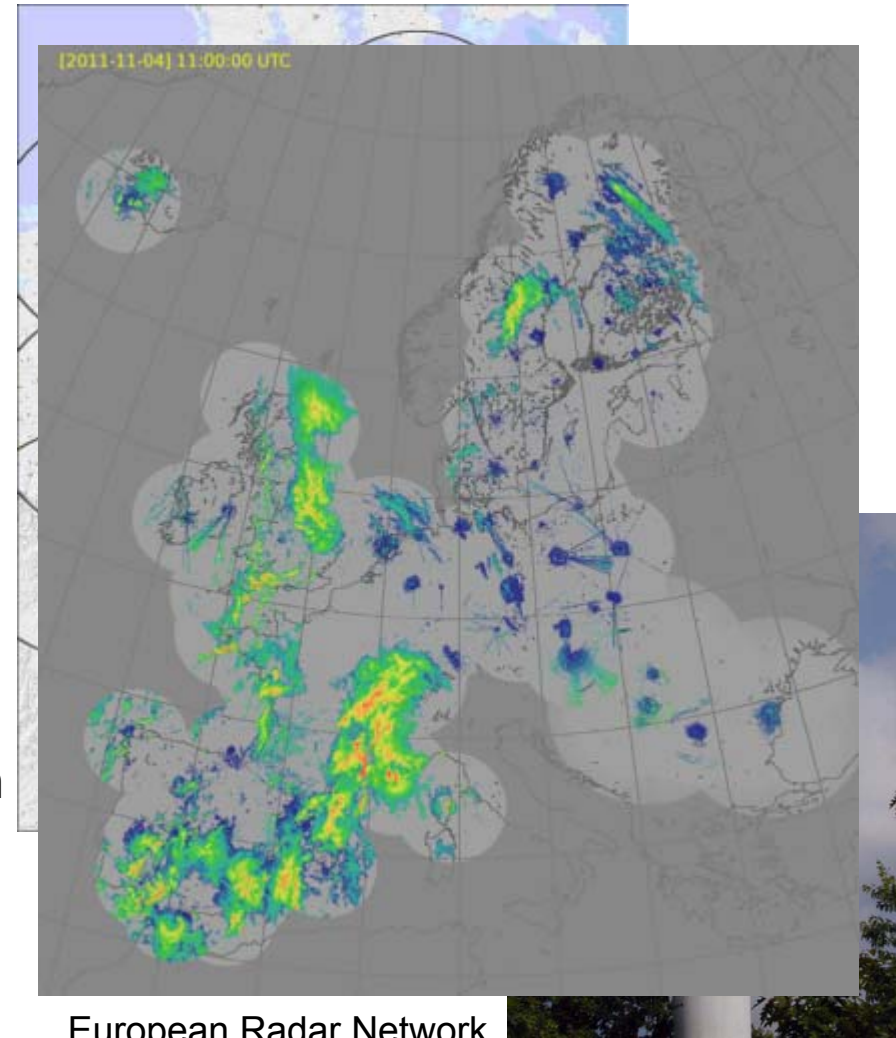
# Motivation



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- High resolution NWP requires observation with a high resolution
- Radar observations will be of great potential for this purpose.
- Current resolution at DWD:
  - 250 m in range (150 km)
  - 1° in azimuth
  - 18 elevation (0.5 – 37°)
  - every 15 min
  - (every 5 min precipitation scan with an elevation above topography)
- Data coverage is very good:  
17 Stations in Germany  
~ 200 in Europe



European Radar Network  
(OPERA)

Hannover





- **RADAR:** acronym standing for **R**adio **D**etection and **R**anging
- Pulses of electromagnetic waves at radio frequency (2-10 GHz, 15-3 cm, S,C,X-Band) are sent and received (reflected by a target) at the same site.



- Each target returns a tiny bit of the transmitted energy
  - Air planes, insects, birds, rain drops, hail ...
- The first application was during the World War 2 to detect air planes
- Measuring the elapsed time between sending and receiving the signal



# Radar Basics



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- Radar Antenna is turning around continuously (1-3 rpm)
- A very short pulse is send ( $\sim 1 \mu\text{s}$ ) and the respond is received ( $\sim 10 \text{ ms}$ )
- After a turn is completed the next elevation is adjusted

## Some facts:

- beam is broadening with distance  
( $\sim 1 \text{ km}^3$  at 100 km)
  - bended due to the refractivity of the atmosphere (normally back to the ground)
  - resolution decreases with distance  
(vertically and azimuthally)
- 
- elapsed time of the signal, azimuth and elevation of the Radar beam yield the location of a target (air craft, rain droplet, insects, etc..)





- Beside the time delay of the signal Weather Radar measures:
  - ❖ **Reflectivity**
    - Estimation of Precipitation Amount (QPE)
  - ❖ **Doppler Velocity** (only for Dopplerised Radar)
    - Measurement of radial wind component
    - Estimation of vertical profile of horizontal wind (VAD)
  - ❖ **Polarimetric Parameters** (only for polarised Radar)
    - Improvement of QPE
    - Distinction of different precipitation types
- This information can be used for NWP in
  - Data assimilation, verification, validation, process studies
- Requires well equipped Radar
  - currently DWD runs 4 DualPol-Doppler-Radar, but will update the whole network in 2013





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# Reflectivity

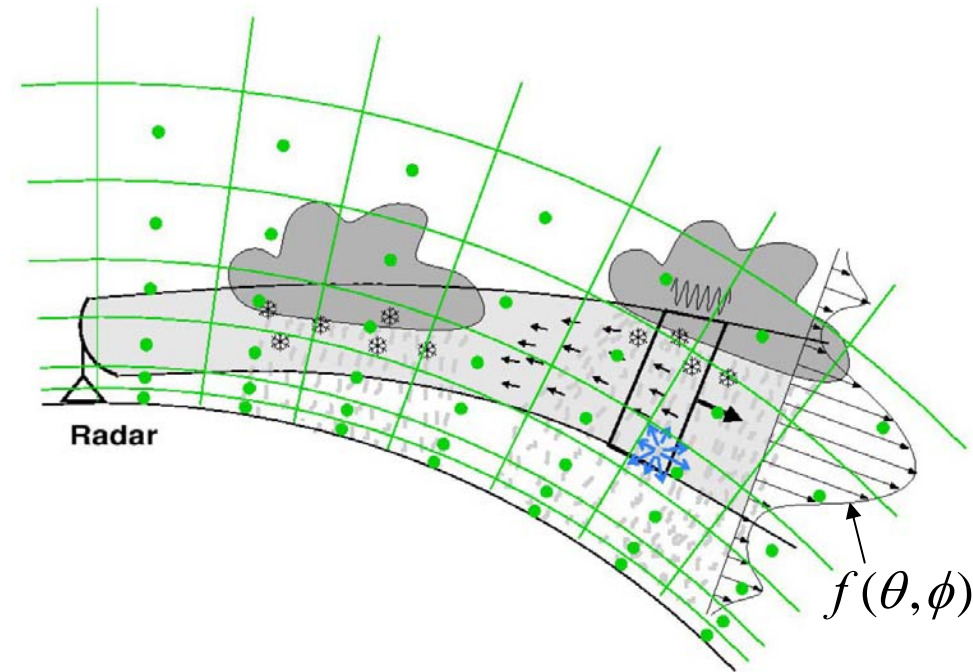


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- Weather Radar measures returning power ( $P_r$ ) of all particles within the radar beam volume (pulse length  $h$  x beam width  $\Delta\theta$ ) with an effective radar cross section  $\sigma_v$
- This yields a Radar Equation of the form

$$P_r = \int P_o \frac{\lambda^2}{(4\pi)^3 r^4} \cdot G^2 \cdot f(\theta, \phi)^2 \cdot \sigma_v dV$$



$P_o$  = emitted power,  $G$ : radar gain,  $\lambda$  wave length,  $r$  distance



# Reflectivity



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This yields:

$$P_r = P_o \frac{\lambda^2 G^2}{64 \pi^3} \cdot \int_r^{r+h/2} \frac{1}{r^2} dr \int_0^\infty N(D) \sigma_B(D) dD \int_0^{2\pi} \int_0^\pi f(\theta, \phi)^2 \sin \theta d\theta d\phi$$
$$\approx P_o \frac{\lambda^2 G^2}{64 \pi^3} \cdot \frac{h}{2r^2} \cdot \eta \cdot \frac{\pi \Delta \theta^2}{8 \ln(2)} = \frac{P_o (\lambda G \Delta \theta)^2 h}{1024 \pi^2} \cdot \frac{\eta}{r^2}$$

From Rayleigh theory ( $D < \lambda/10$ ):

$$\eta = \frac{\pi^5}{\lambda^4} \left| \frac{\varepsilon - 1}{\varepsilon + 2} \right|^2 \cdot \sum D^6 = \frac{\pi^5}{\lambda^4} \cdot |K|^2 \cdot z$$

With:

$\eta$ : Radar reflectivity

$z$ : Reflectivity

$\varepsilon, K$ : dielectric constant  
(variable for water (0.93)  
and ice (0.18))

This yields:

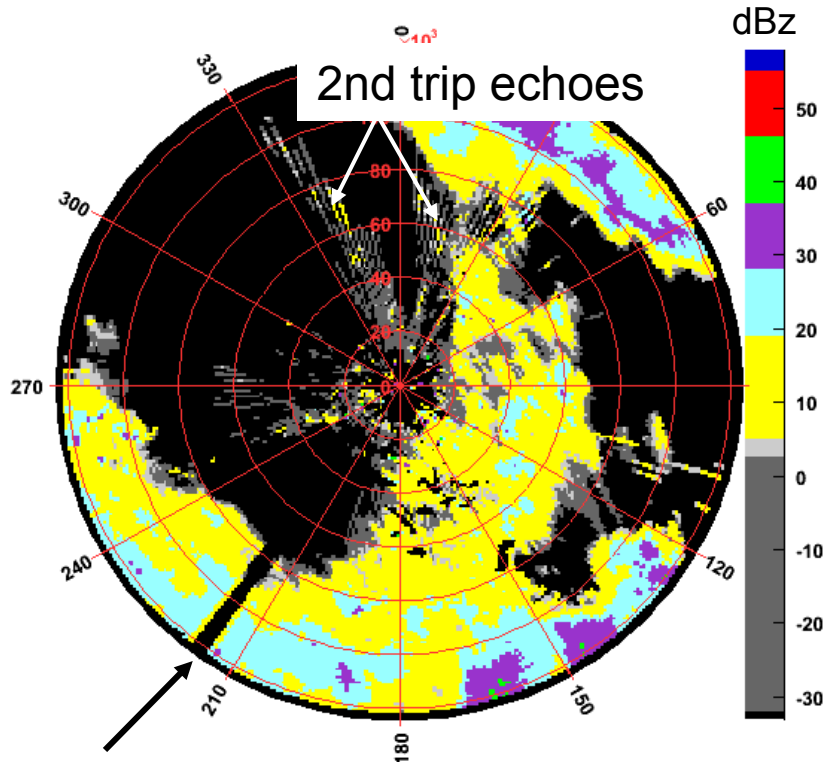
$$P_r = \frac{C |K|^2}{r^2} \cdot z$$



# Reflectivity



PPI of Reflectivity (lowest elevation)



Beam blockage due to obstacles

Beside this there are a lot more sources of error





Measure of  $z$  might be affected by

- Incorrect calibration
- Attenuation → underestimation of  $z$
- Anomalous beam propagation due to super- or under-refraction → over- or underestimation of  $z$ , erroneous localisation
- Second-Trip-Echoes, Echoes from side lobes, multi path scattering
- Non Rayleigh targets (  $D \sim \lambda$  )
- Misinterpretation of snow reflectivity
- „Non rain echoes“ (birds, insects,...)
- Brightband → melting snow leads to huge overestimation
- ...





- Scattering and absorption at hydrometeors and atmospheric gases
- Occurs mainly behind strong precipitation and in case of wet radome (Radar globe)
- Can be calculated by

## Bouguet-Lambert-Beer'sches Law

$$P(s) = P(0) \exp(-\delta(s)) = P(0) \exp\left(-\int_0^{\infty} \sigma_e(s') ds'\right)$$

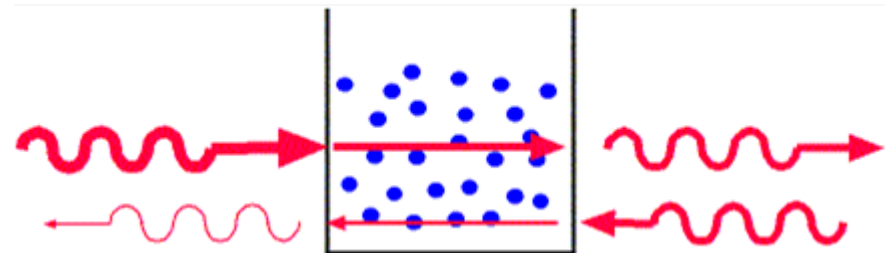
**P** - Power [W]

$\sigma_e$  - extinction coefficient [ $\text{m}^{-1}$ ]

**s** - range [m]

$\delta$  - optical thickness

Attenuation will happen twice





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# Bright Band Effect



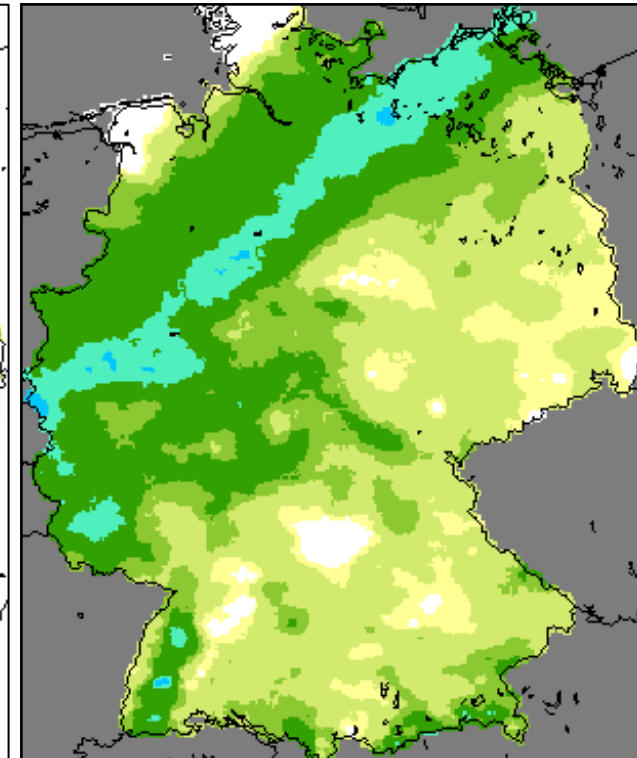
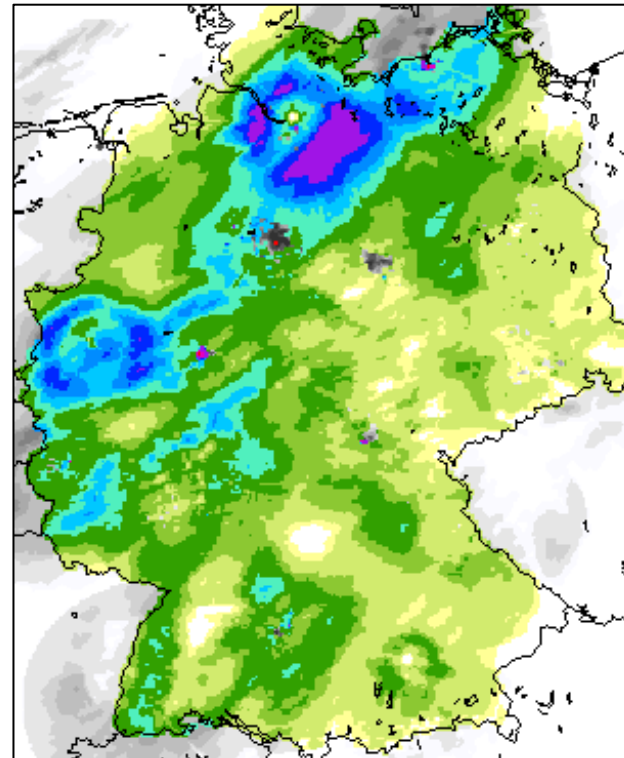
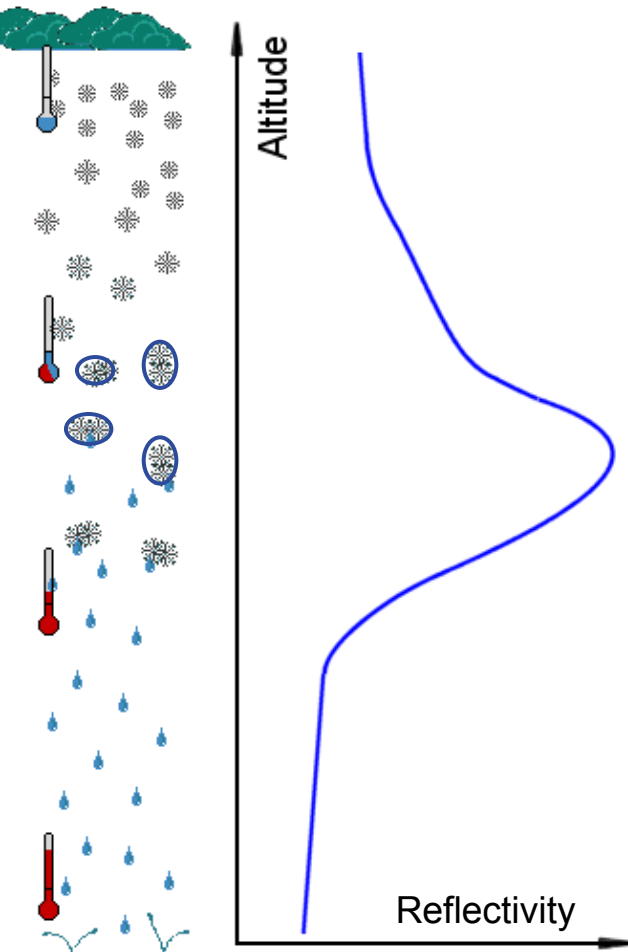
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24h Precipitation sum

Radar estimation

Gauge measurement



19. November 2006

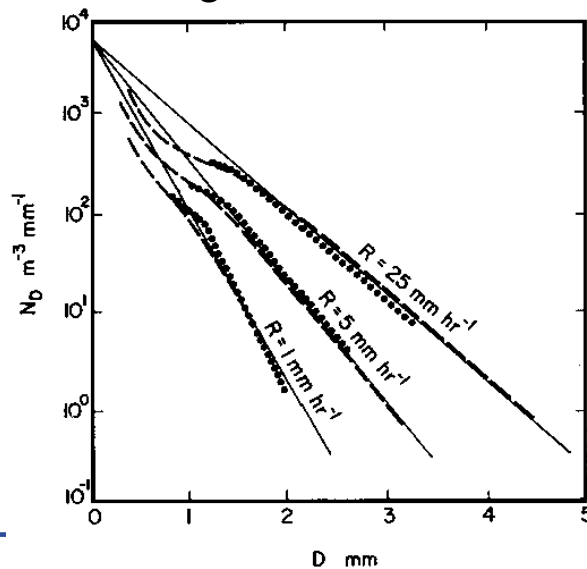
(wikipedia.com)



# Reflectivity → QPE



- Most users are not interested in Reflectivity
- Transformation of  $z$  in precipitation rate ( $R$ ) is applied
- $z$  and  $R$  are both two different moments of the drop size distribution
  - $z \sim D^6$  and  $R \sim D^{3.7} \rightarrow$  non linear relationship  $z=aR^b$
  - Using Marshall-Palmer DSD yields  $z=200R^{1.6}$
  - $z$ - $R$  relationship very variable, depends on weather conditions
  - QPE using  $z$ - $R$  relation is uncertain (polarisation might be improving)



$$N(D) = N_0 e^{-\Lambda D}$$
$$\Lambda = 41R^{-0.21}$$
$$N_0 = 0.08 \text{ cm}^{-4}$$

(Marshall & Palmer, 1948)







- Both  $z$  and  $R$  can be used in DA
  - MeteoFrance: 1dVar using  $z$  → retrieving  $T, q$  to be used in 3(4)dVar
  - UKMO and COSMO: Latent heat nudging (LHN) of  $R$
  - Applying a Radar forward operator to obtain modelled  $z$  and estimation of observation increment → could be used in LETKF approach





## Assimilation of Radar-Derived Precipitation by Latent Heat Nudging

- **Required:** relation: precipitation rate  $\leftrightarrow$  model variables  
(observed) (info required by nudging)  
precipitation  $\leftrightarrow$  condensation  $\leftrightarrow$  release of latent heat

→ **Assumption:** vertically integrated latent heat release  $\propto$  precipitation rate

- **Approach:** modify latent heating rates such that the model responds by producing the observed precipitation rates  
→ Latent Heat Nudging (LHN)

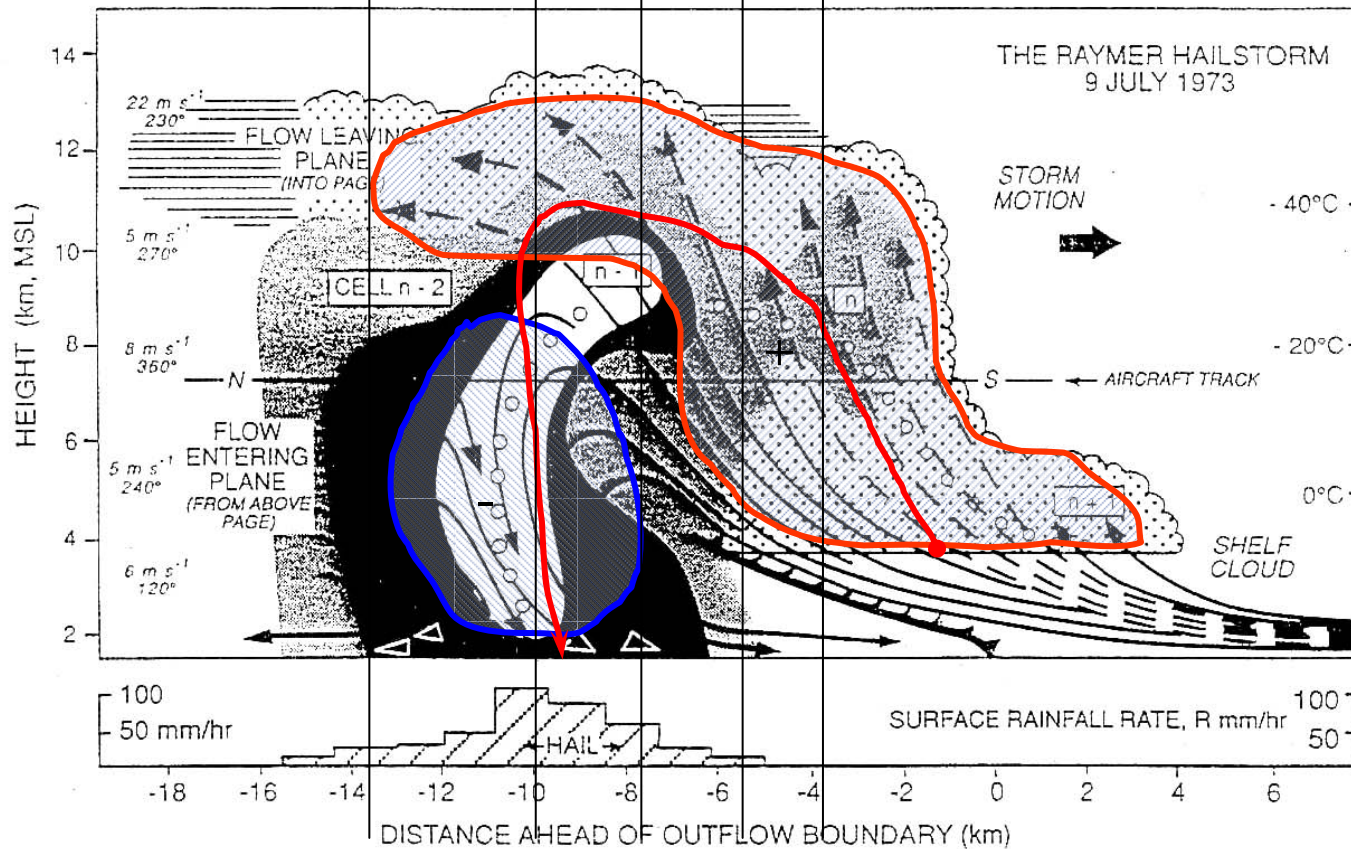
$$\frac{\partial T}{\partial t} = F(T) + \left( \frac{\partial T}{\partial t} \right)_{nudging} + \left( \frac{\partial T}{\partial t} \right)_{LHN}$$
$$\Delta T_{LHN} = (\alpha - 1) \cdot \Delta T_{LH} \quad \text{with} \quad \alpha = \frac{RR_{obs}}{RR_{ref}}$$

+ adjustment of specific humidity to maintain relative humidity





Correlation:            0        <0        low    max    low        0



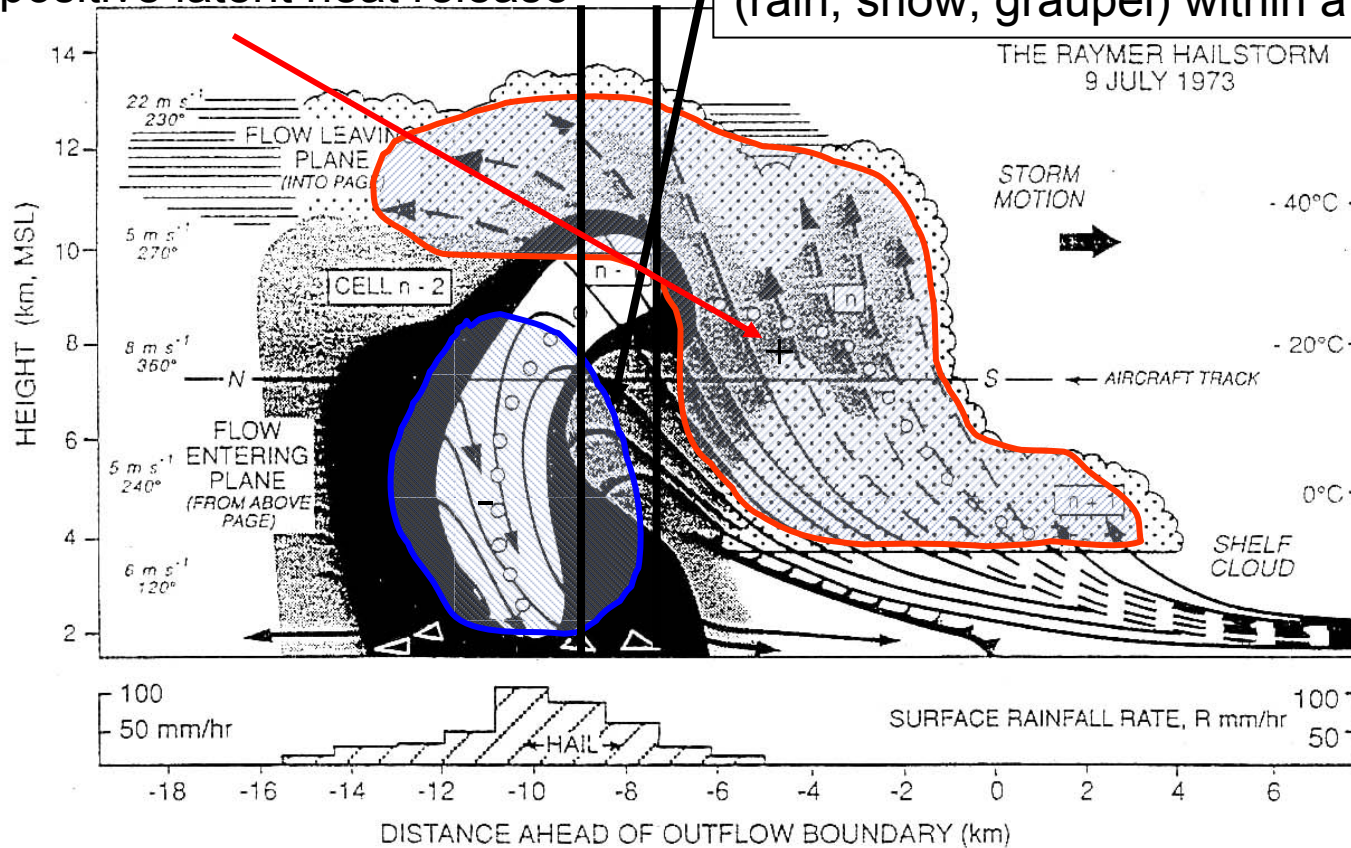
(R. A. Houze, Jr.: Cloud Dynamics, International Geophysics Series Vol. 53)





Treatment only of model layers with positive latent heat release

Reference Precipitation:  
Vertical mean of precipitation flux (rain, snow, graupel) within a volume



(R. A. Houze, Jr.: Cloud Dynamics, International Geophysics Series Vol. 53)





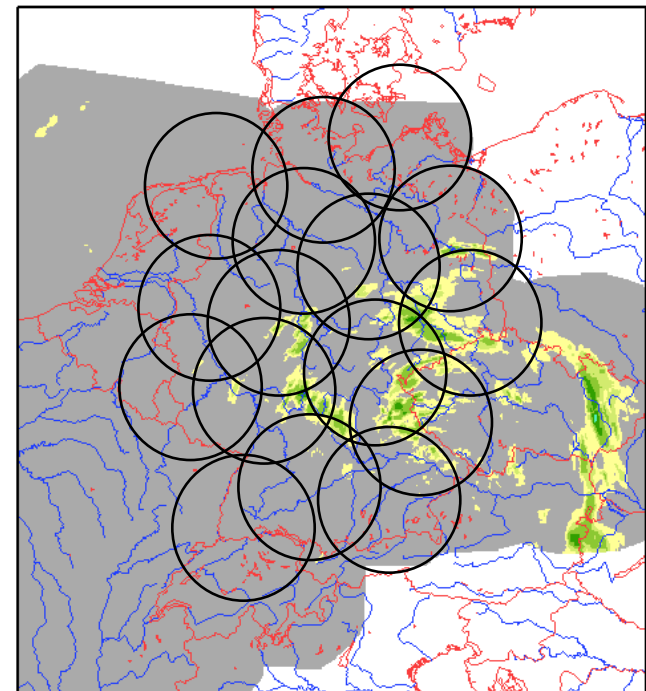
## Radar data coverage

- Currently
  - 16 German Doppler radar stations
  - 2 Dutch stations
  - 2 Belgian stations
  - 9 France stations
  - 3 Swiss stations
  - 2 Czech station
- Shortly extended by
  - 1 German station (Memingen)
  - 2 Polish stations

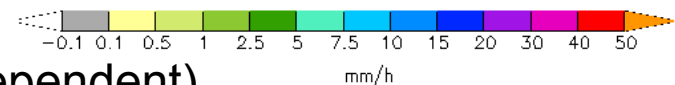
RADAR COMPOSITE

valid: 26 APR 2011 12 – 13 UTC

1h PRECIPITATION



Mean: 0.0580894 Min: 0 Max: 6.53501



R is derived using a 4 class z-R relation (storm dependent)



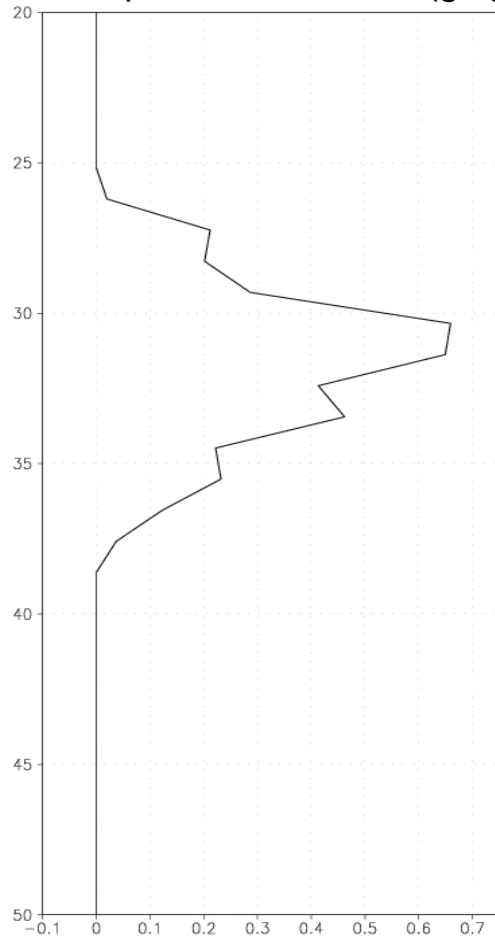
# Reflectivity → LHN



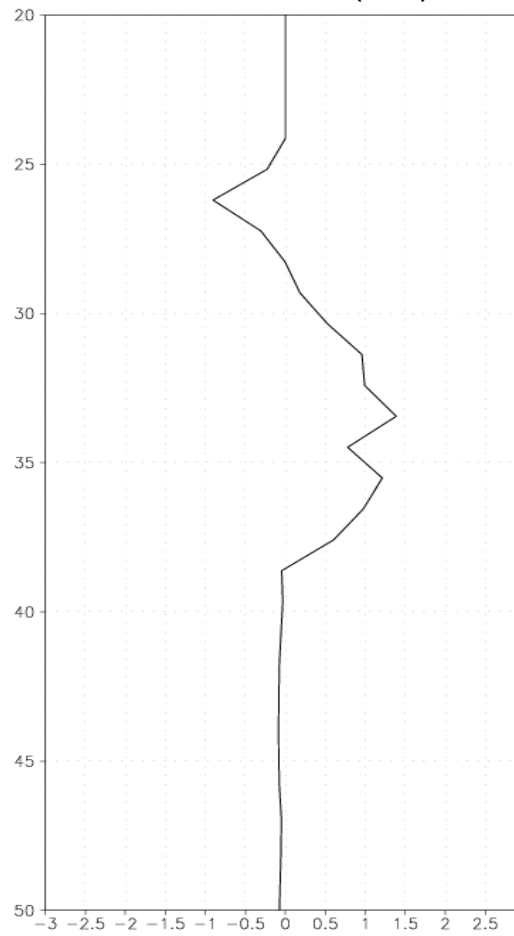
## How does it works?

Vertical profiles:

cloud liquid water content (g/kg)



latent heat release (K/h)



temperature increment (K)



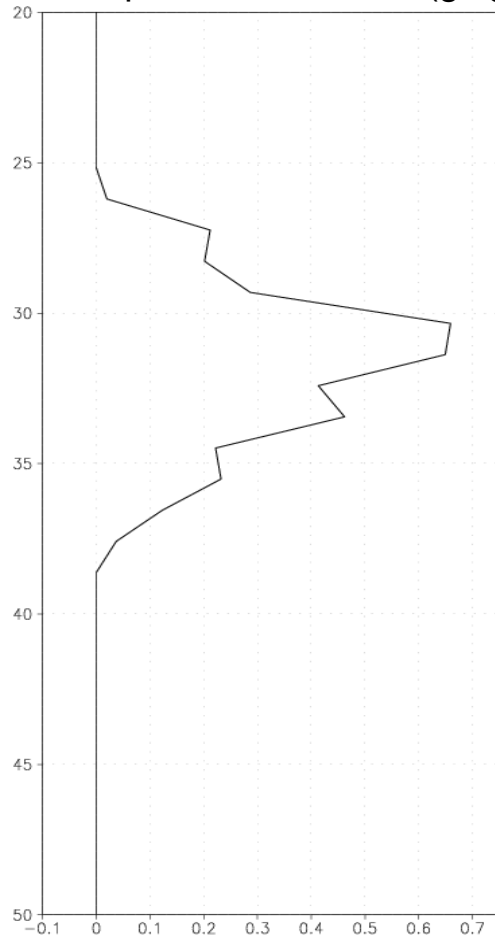
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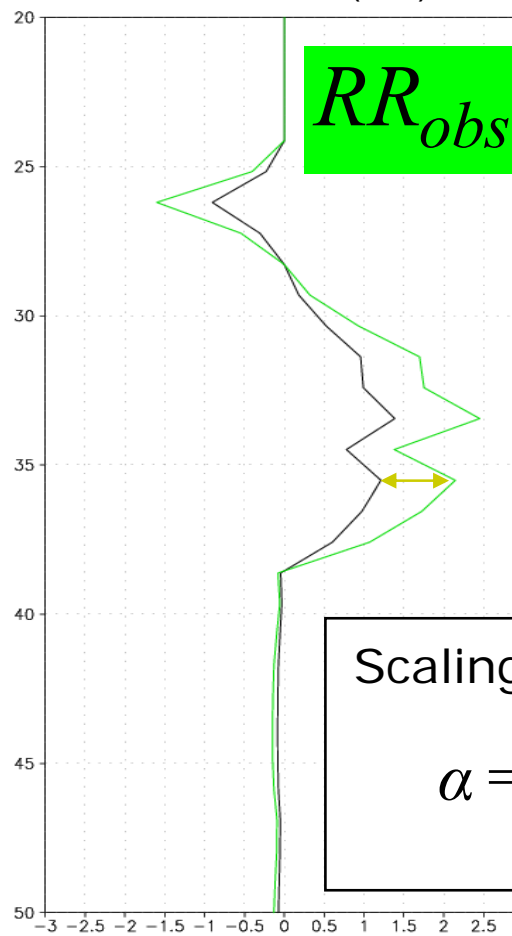
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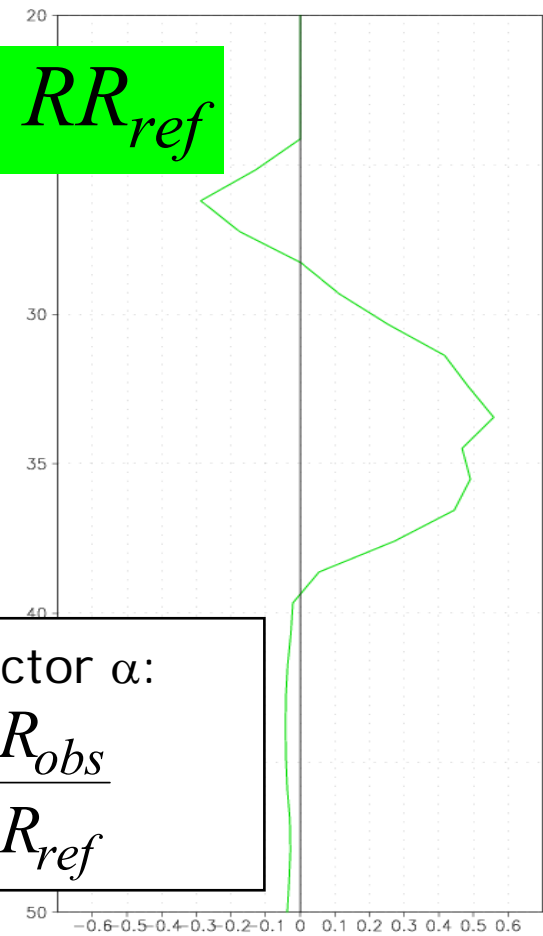


$$RR_{obs} > RR_{ref}$$

Scaling factor  $\alpha$ :

$$\alpha = \frac{RR_{obs}}{RR_{ref}}$$

temperature increment (K)

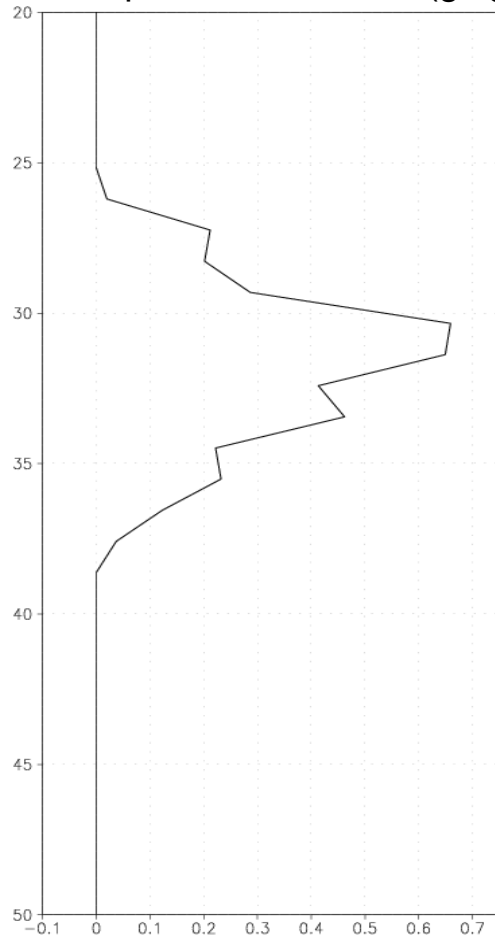


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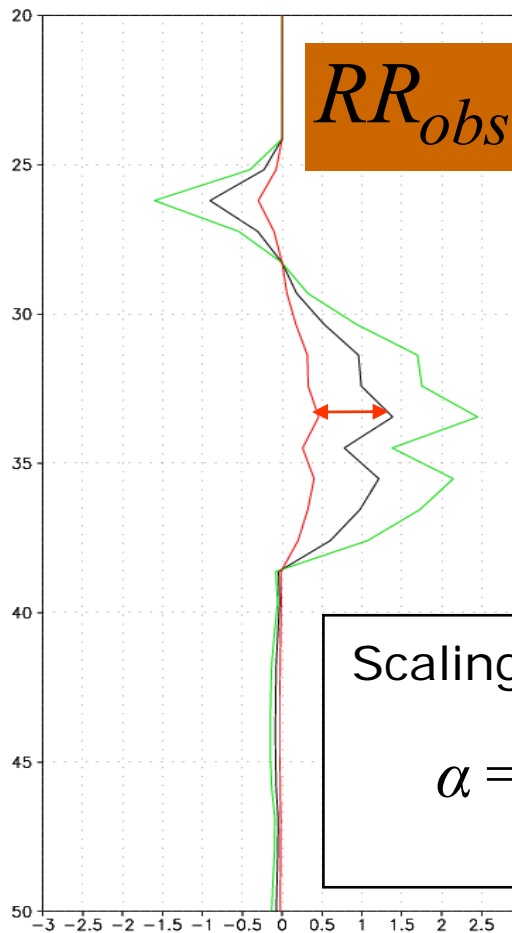


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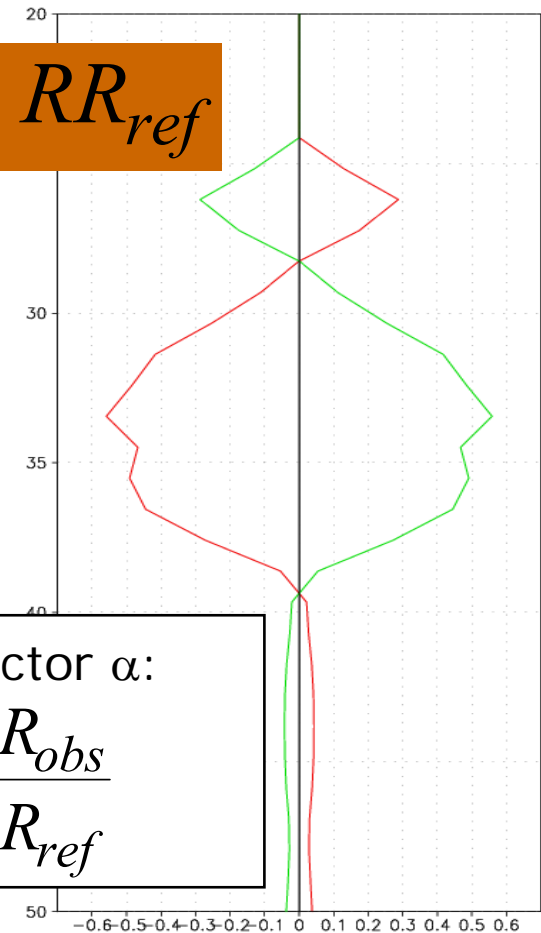
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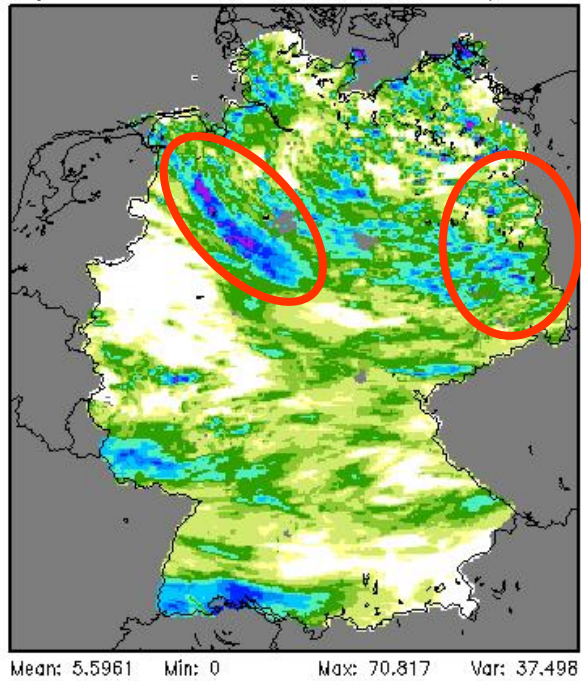
# Reflectivity → LHN



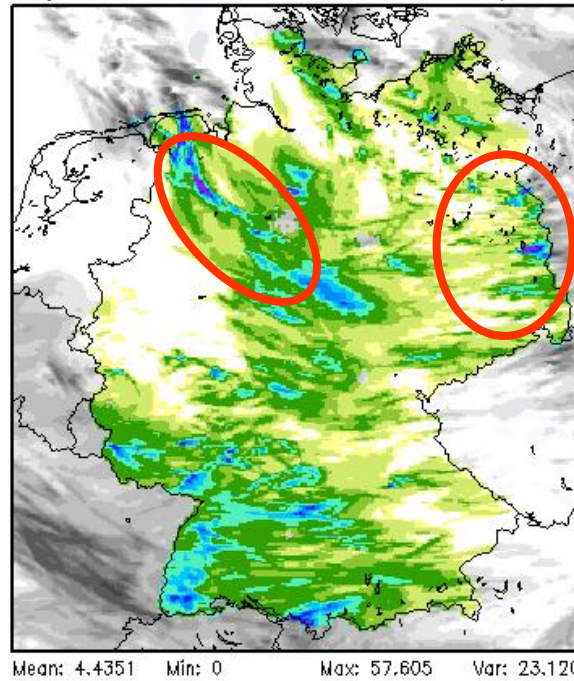
24H precipitation sum: 26.08.2006 (6 UTC – 6 UTC)

Assimilation

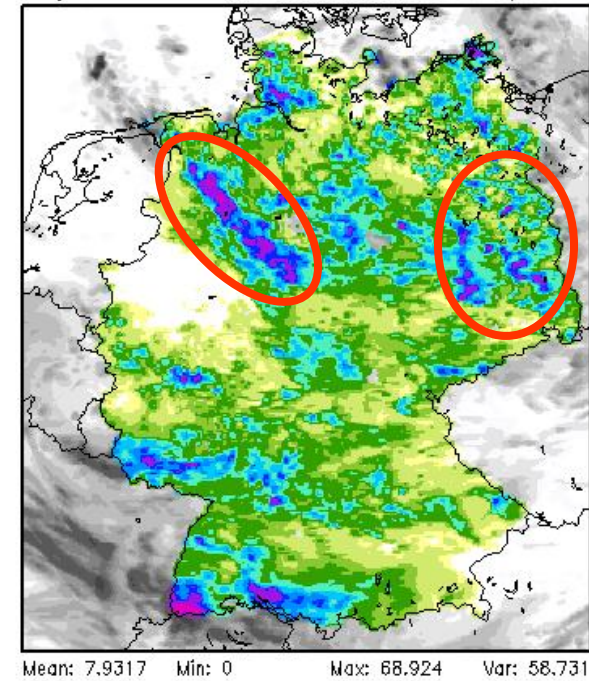
Radar-OBS



No LHN



LHN



# Reflectivity → LHN



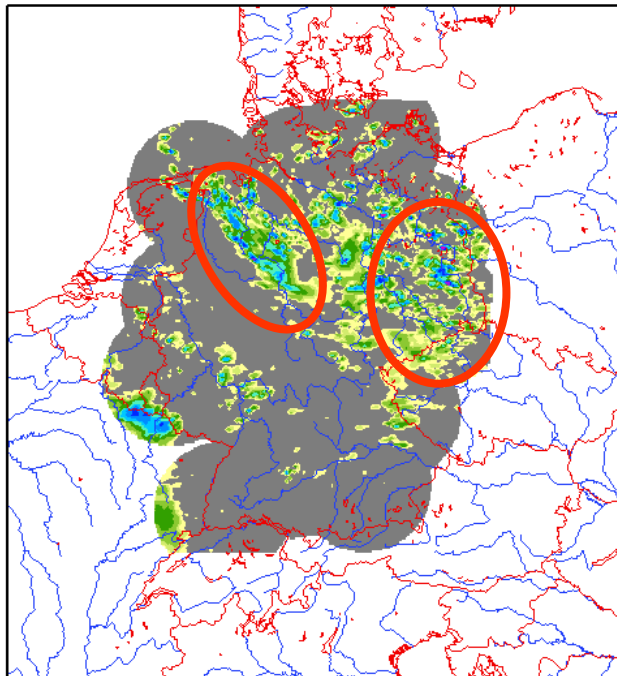
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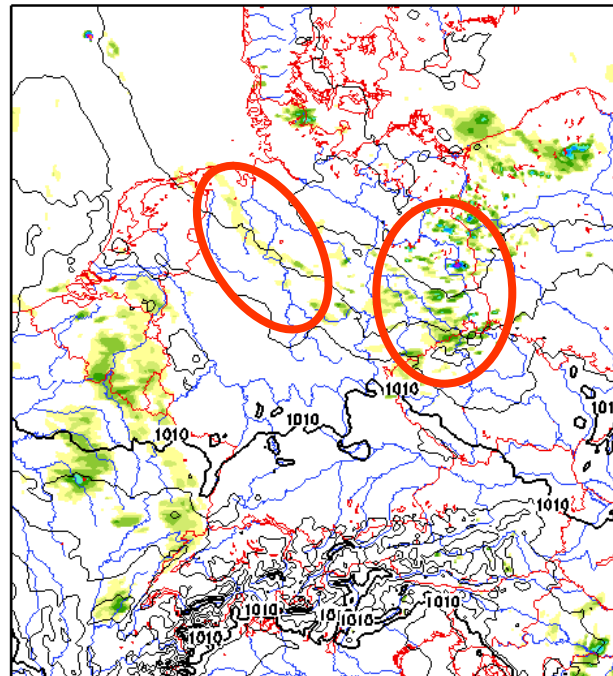
Animation of 1H precipitation sum 26. August 2006

Free Forecast 12 UTC + 1 H  
(Assimilation till 12:30 UTC)

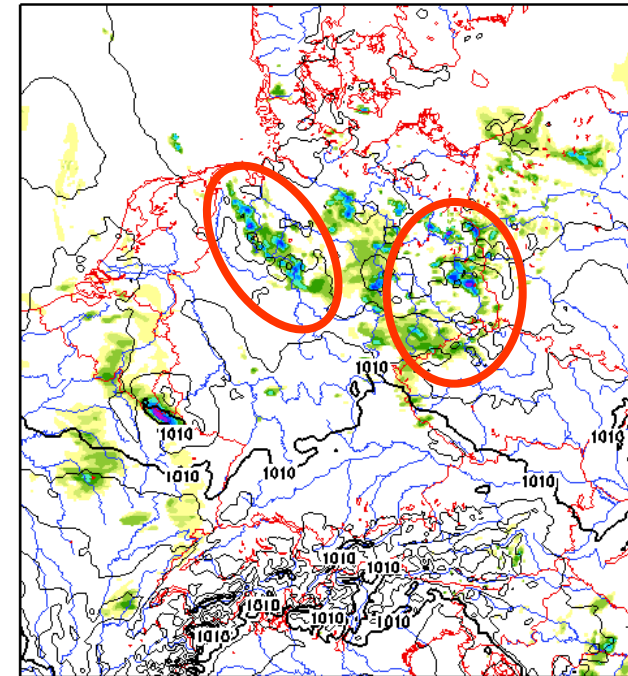
Radar-OBS



No LHN



LHN



# Reflectivity → LHN



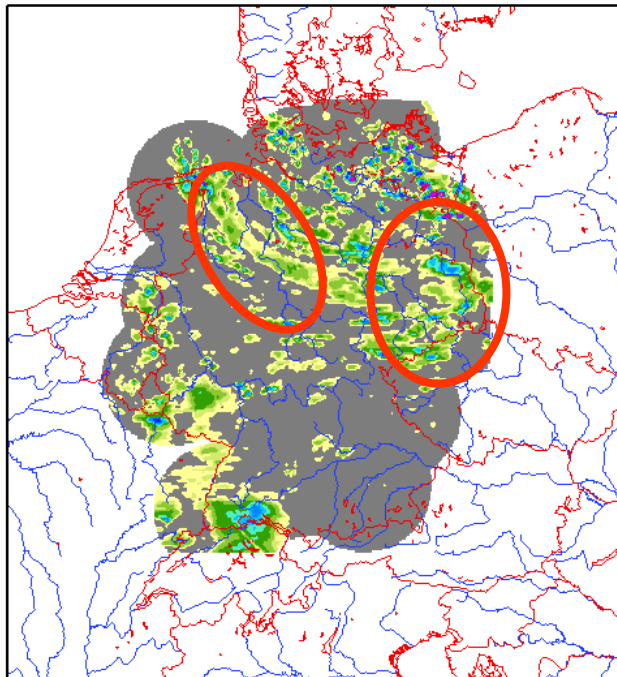
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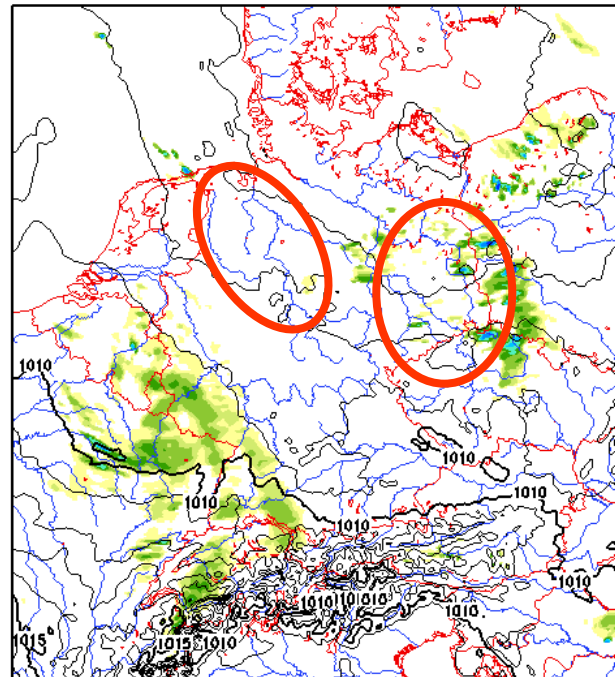
Animation of 1H precipitation sum 26. August 2006

Free Forecast 12 UTC + 4 H

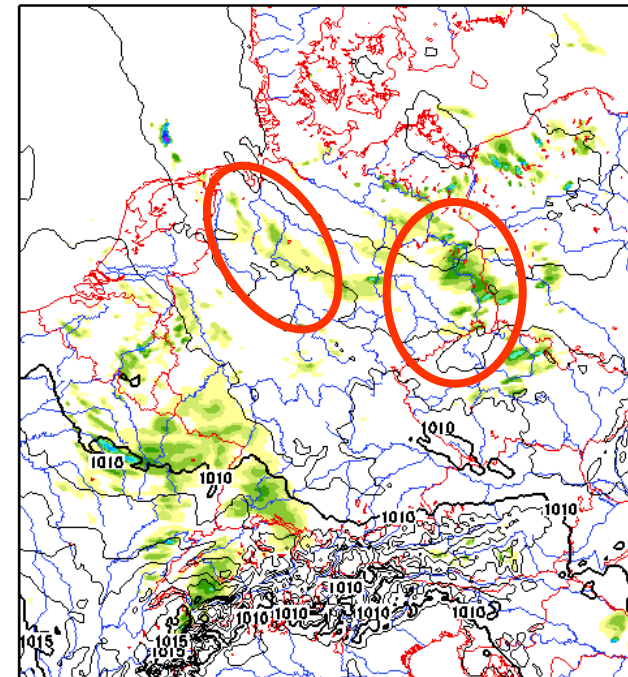
Radar-OBS



No LHN



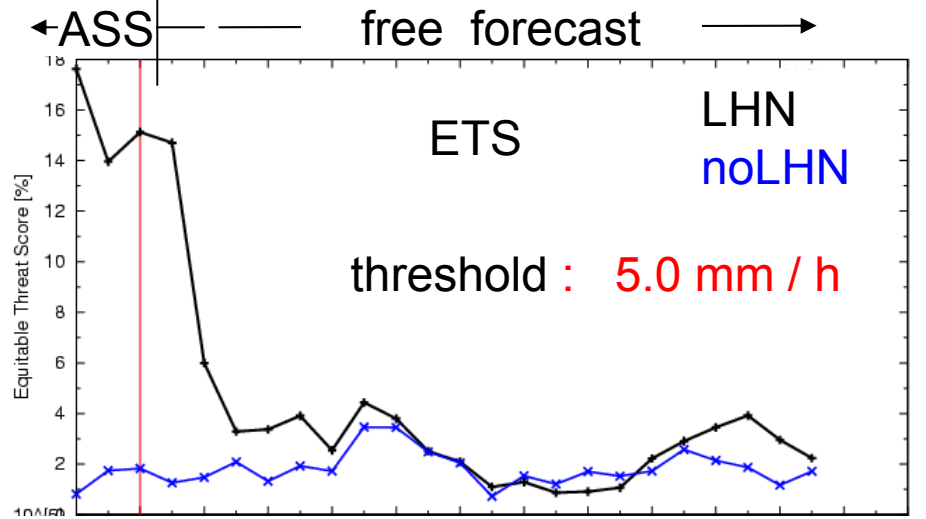
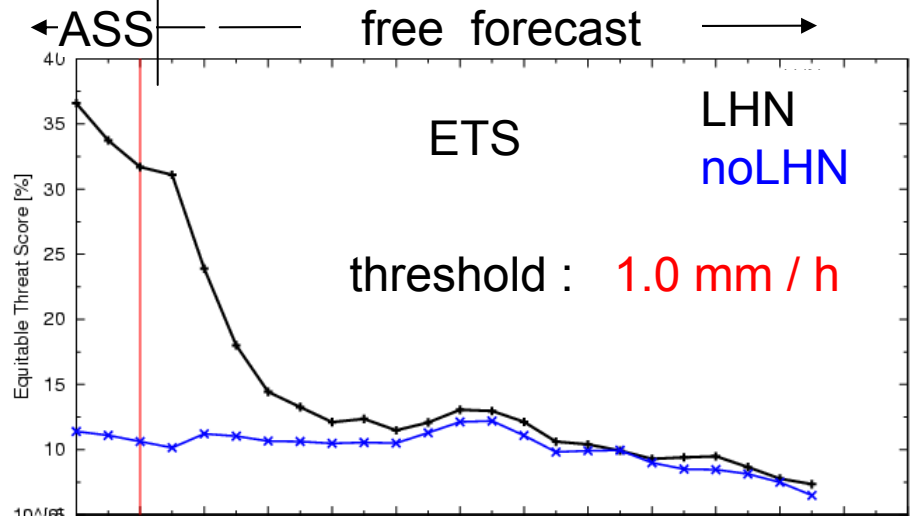
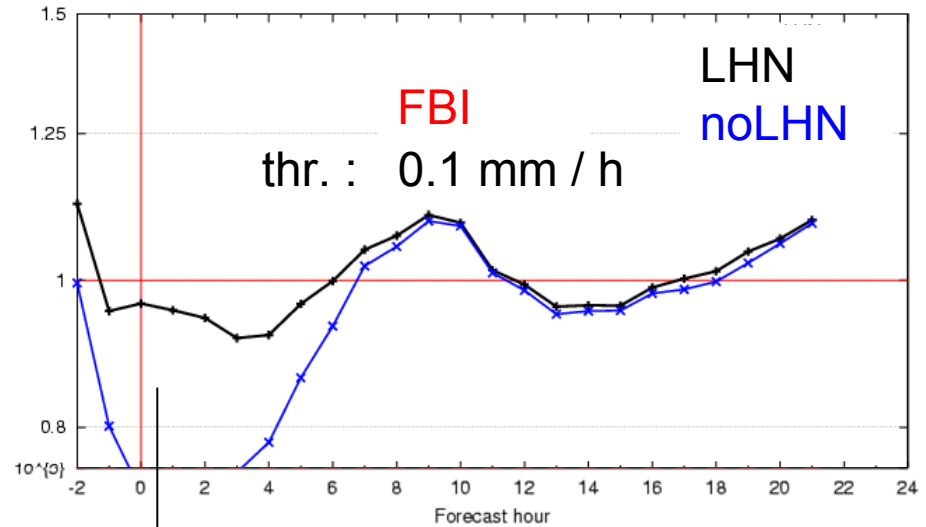
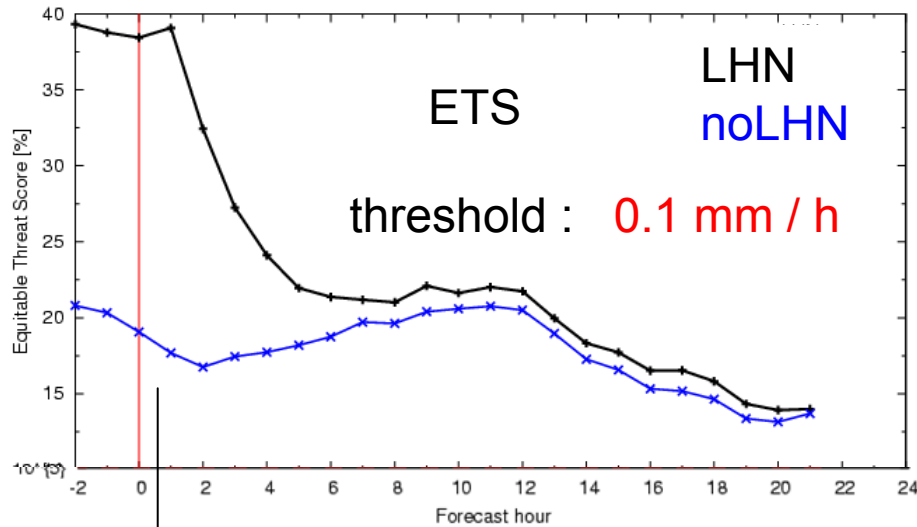
LHN





# Reflectivity → LHN

15 – 30 August 2006, 00 and 12 UTC runs (32 forecasts); threshold : 0.1 mm / h





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# Radial Wind Component



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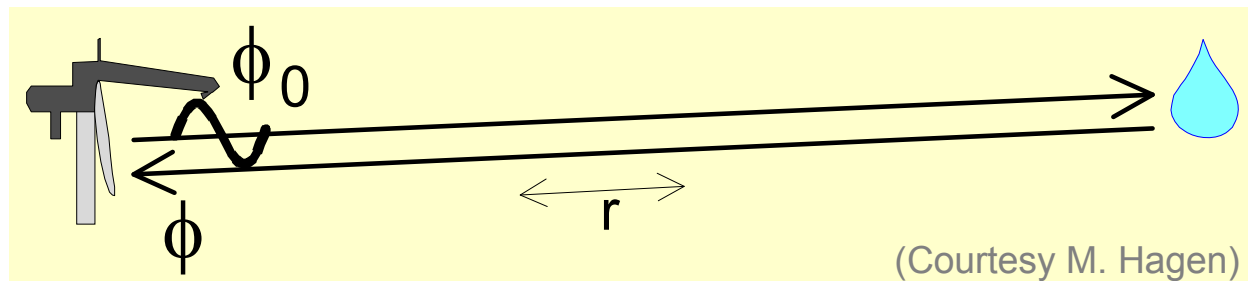


- A so called Doppler Radar is able to measure the phase of the radio wave.
- Moving targets will produce a phase shift due to the Doppler effect
- This shift can be detected and the velocity along the beam can be measured (radial component of the wind vector)

$$\phi = \phi_0 + \frac{4 r \pi}{\lambda} \longrightarrow \frac{\Delta \phi}{\Delta t} = \frac{4 \pi}{\lambda} \cdot \frac{\Delta r}{\Delta t} = \frac{4 \pi}{\lambda} \cdot v_r$$

$$v_r = \frac{\Delta \phi}{\Delta t} \cdot \frac{\lambda}{4 \pi}$$

$\Delta \Phi$ : phase shift  
 $\lambda$ : wave length  
 $\Delta t$ : pulse repetition time  
 $r$ : distance



(Courtesy M. Hagen)



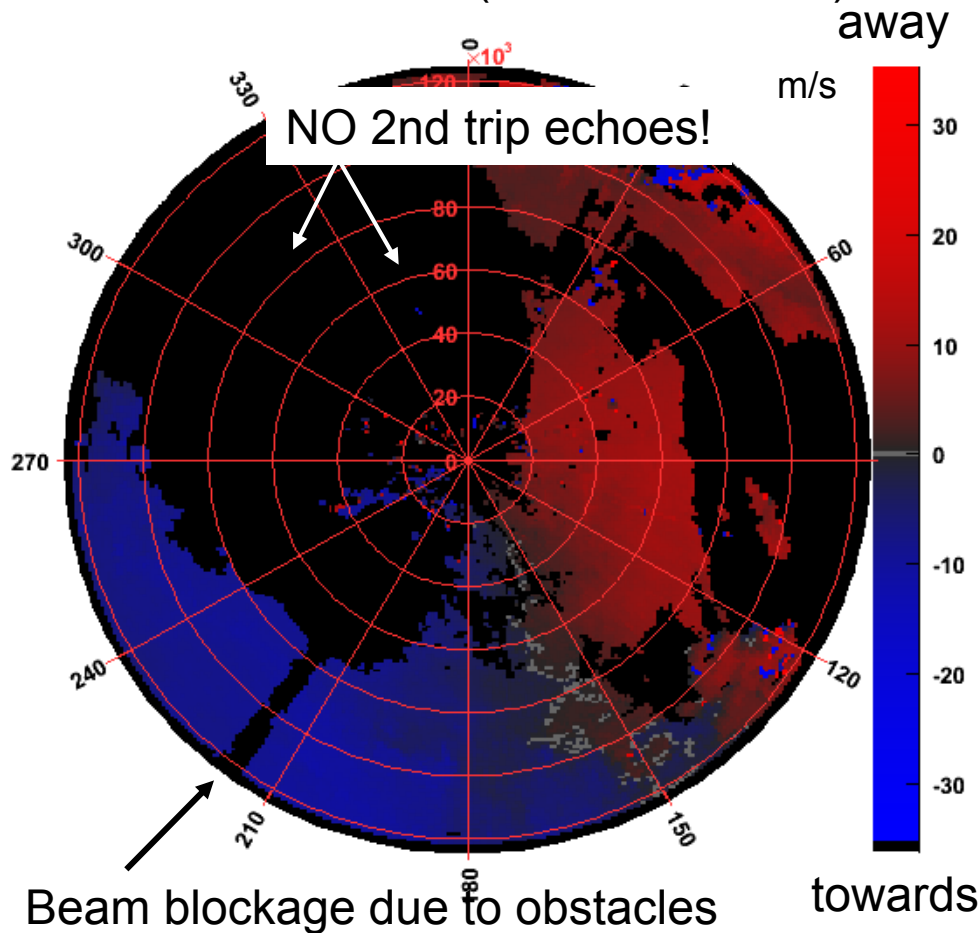
# Radial Wind Component



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PPI of radial wind (lowest elevation)



Radial wind volumes can be used for:

- clutter filtering (stationary ground clutter, but not wind mills)
- 2nd trip detection
- Estimation of vertical profile of horizontal wind (VAD)
- directly used for DA
- Hazard warning: meso cyclone detection



# Radial Wind Component



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- Doppler Dilemma:
  - Aliasing effect leads to an unambiguous velocity interval:
  - Nyquist velocity:  $v_{r \max} = \pm \frac{\lambda}{4\Delta t}$
  - Max Range:  $r_{\max} = \frac{c\Delta t}{2}$
- A higher range leads to a smaller Nyquist velocity and vice versa

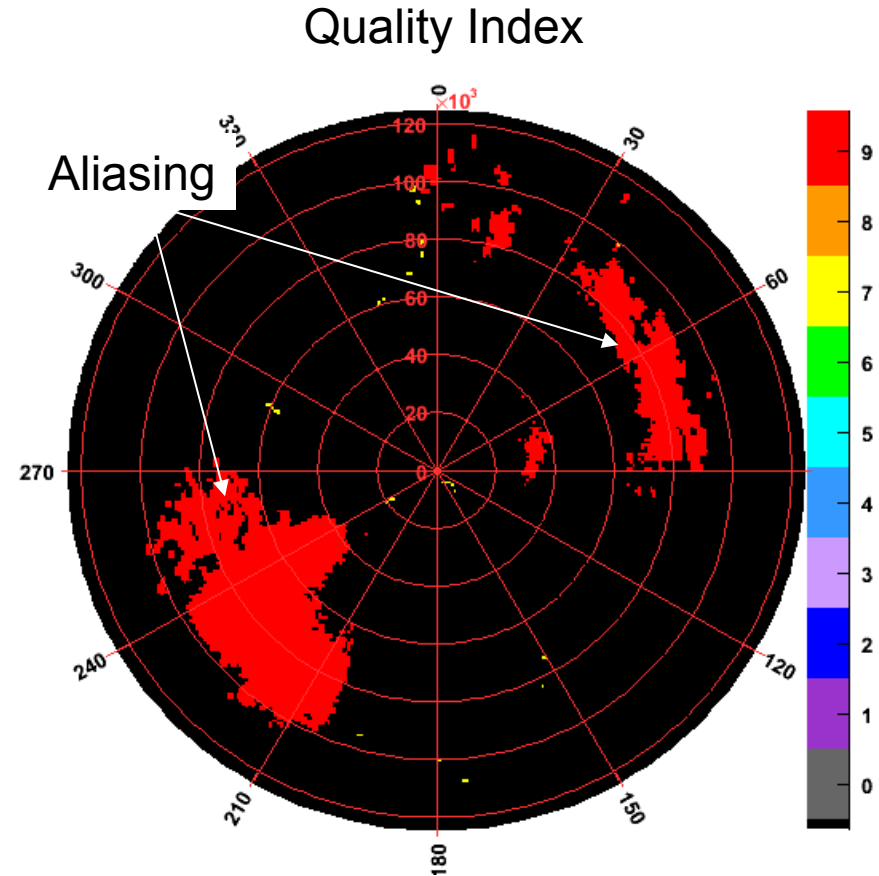
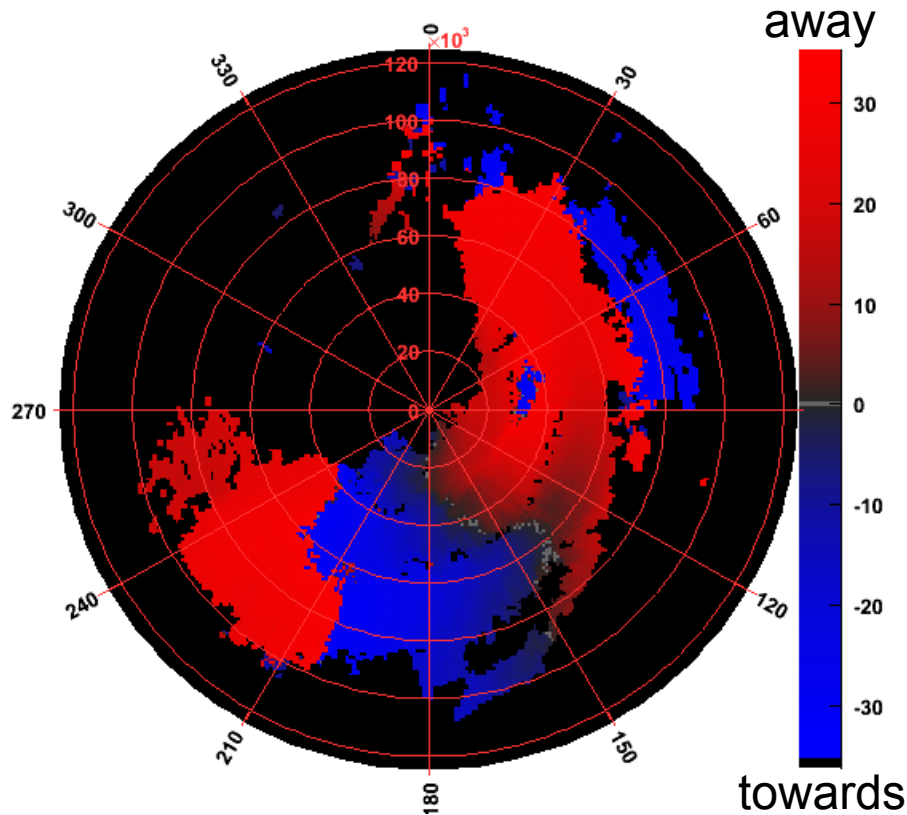




# Radial Wind Component



→ Example for Aliasing effect (easy one)



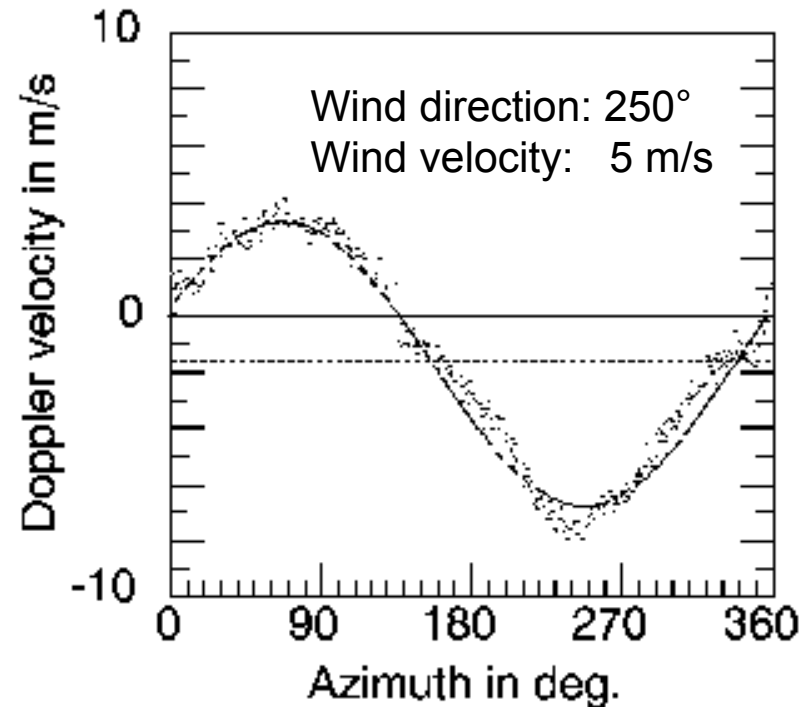
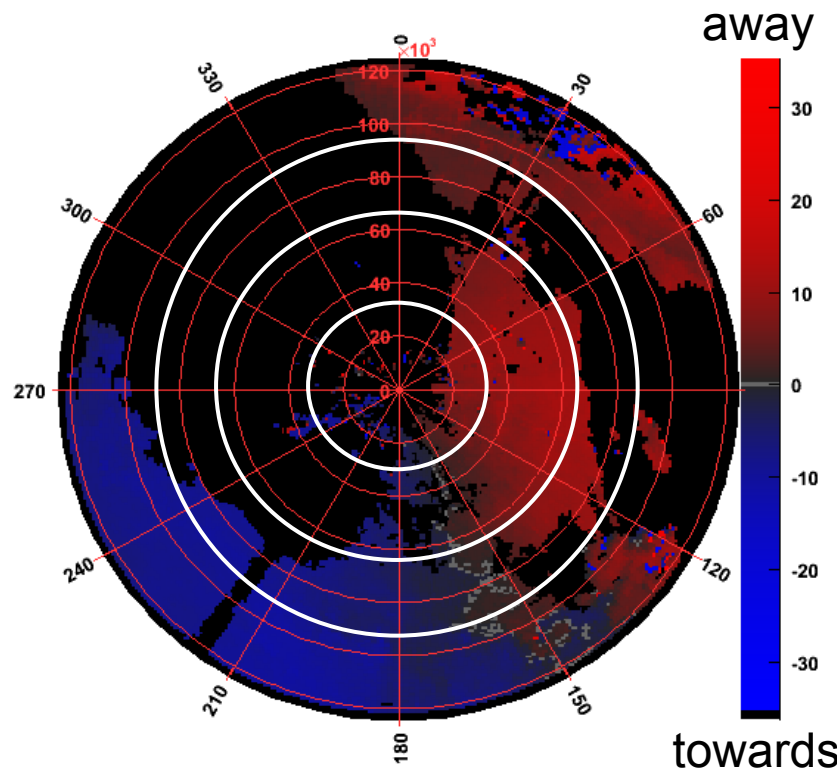
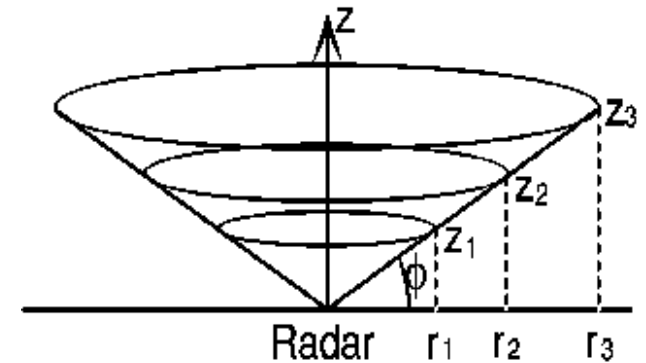
(Nyquist velocity = 32 m/s)



# Radial Wind Component - VAD



- at each height layer (500 m bins), a sinus curve is fitted to the measured radial wind components which depends on azimuth  
→ velocity & direction of mean wind vector
- Assumption: homogeneous wind field !



# Radial Wind Component -VAD

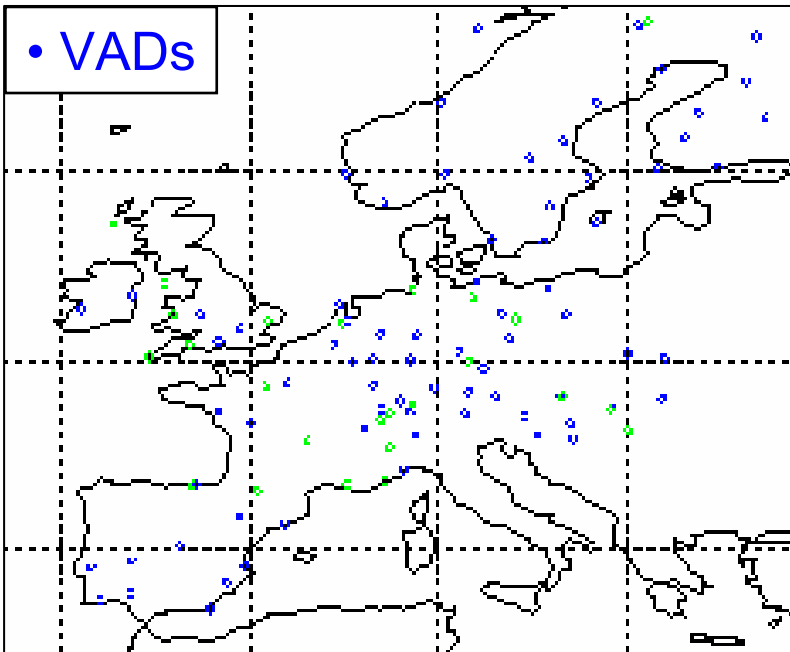


Deutscher Wetterdienst  
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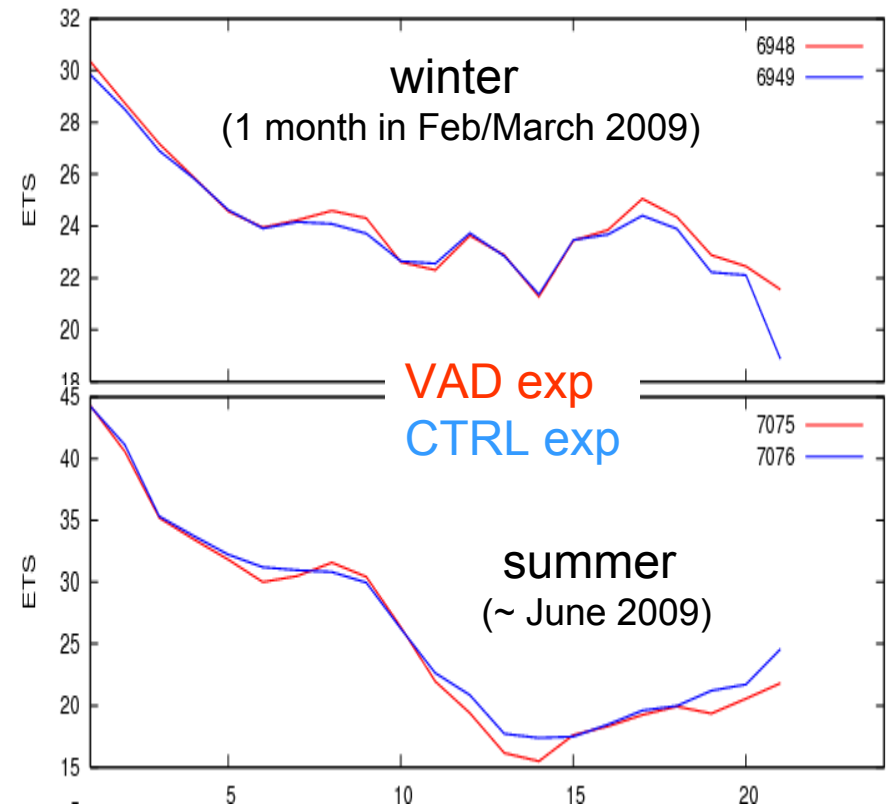


95 VAD stations available:

50 on whitelist, i.e. used actively  
(some height ranges on blacklist)



ETS, threshold 0.1 mm, 00-UTC runs



- altogether neutral results
- not used operationally because of monitoring costs
- VAD will lose much of the information, anyway



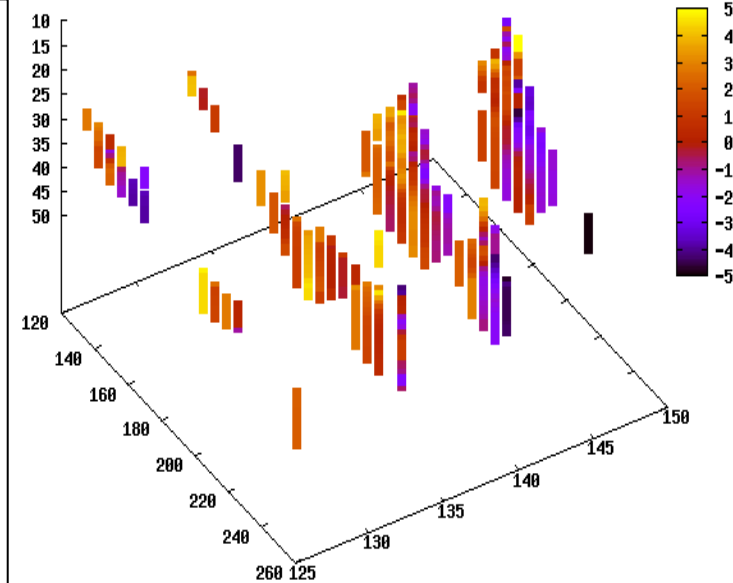
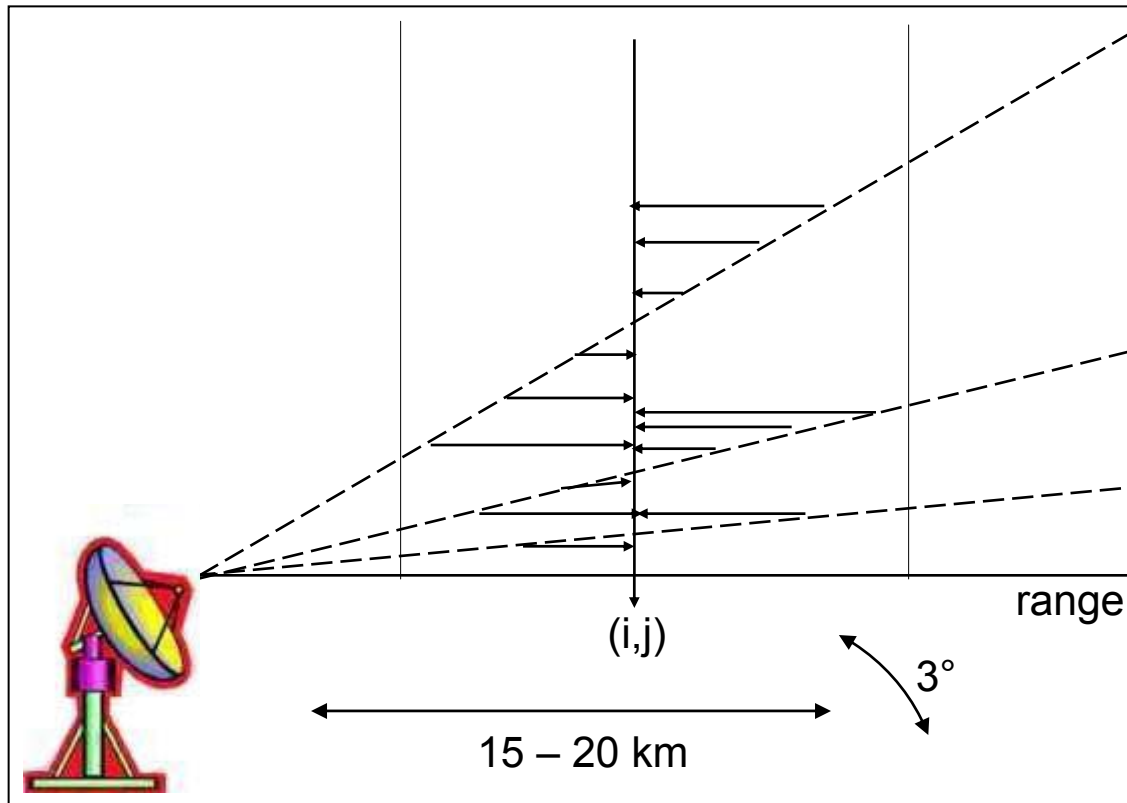
# Radial Wind Component → Nudging



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- compute differences (obs – model) of radial wind component
- assign (shift) to specified model grid points  
→ vertical profiles of increments or pseudo obs of radial wind component
- ingest in nudging



→ first tests soon





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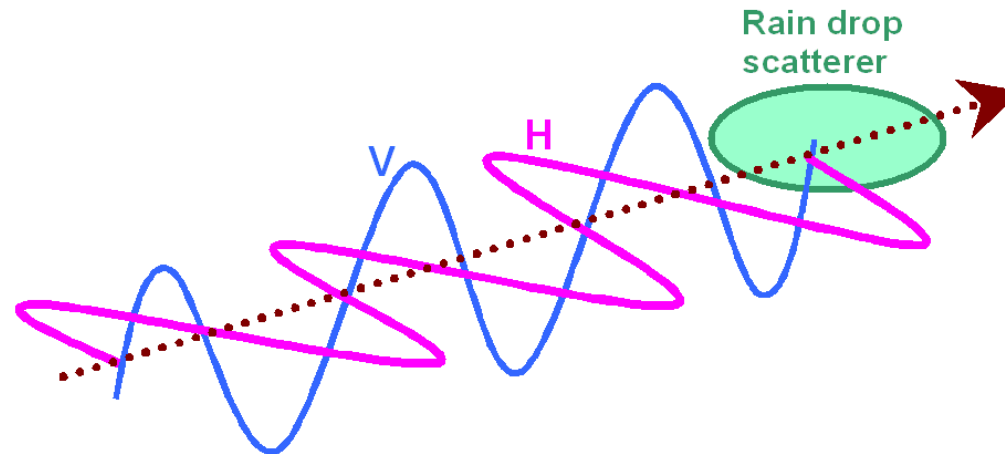
# Polarisation



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- Weather Radar normally send waves in horizontal polarisation (E field looks in the horizontal)
  - Good for liquid hydrometeor (flat objects)
  - Less good in case of tumbling hail stones (elevated objects)
- Better to send separate waves with both horizontal and vertical polarisation?



→ Instead of  $z$  and  $\phi$  measuring of  $z_h, z_v, \phi_h, \phi_v$   
→ number of combinations:  $z_{DR}, LDR, \rho_{HV}, k_{DP}, \phi_{DP}, \dots$



# Polarisation



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- Can be used for
  - Distinction of different hydrometeors (hail, snow, rain)
  - Improvement of Quality-Control (bright band, clutter)
  - Improvement of QPE (better z-R relation)
  - First attempts to assimilate at MeteoFrance





1. Motivation
2. Basics on Radar meteorology
3. Radar measurement and its assimilation
  - Reflectivity
    - LHN
  - Radial Wind Component
    - VAD
    - Nudging
  - Polarisation
4. Brief introduction on Radar Forward Operator (for the LETKF era)







## → assimilate 3-D radial velocity and 3-D reflectivity directly

Uli Blahak (DWD), Yuefei Zeng, Dorit Epperlein (KIT Karlsruhe)

### 1. implement full, sophisticated observation operators

Mie- or Rayleigh-scattering,

combined with different formulations of the effective refractive index of the hydrometeors (mixtures of ice, air, and water)

→ beam attenuation (damping) due to hydrometeors

→ online radar beam propagation (depend. on refractivity)

→ beam smoothing / broadening

→ hydrometeor fall speed (for radial velocities)

→ (superobbing, thinning, obs errors, writing to NetCDF feedback files)

### 2. apply / test sufficiently accurate and efficient approximations

→ by looking at the simulated obs

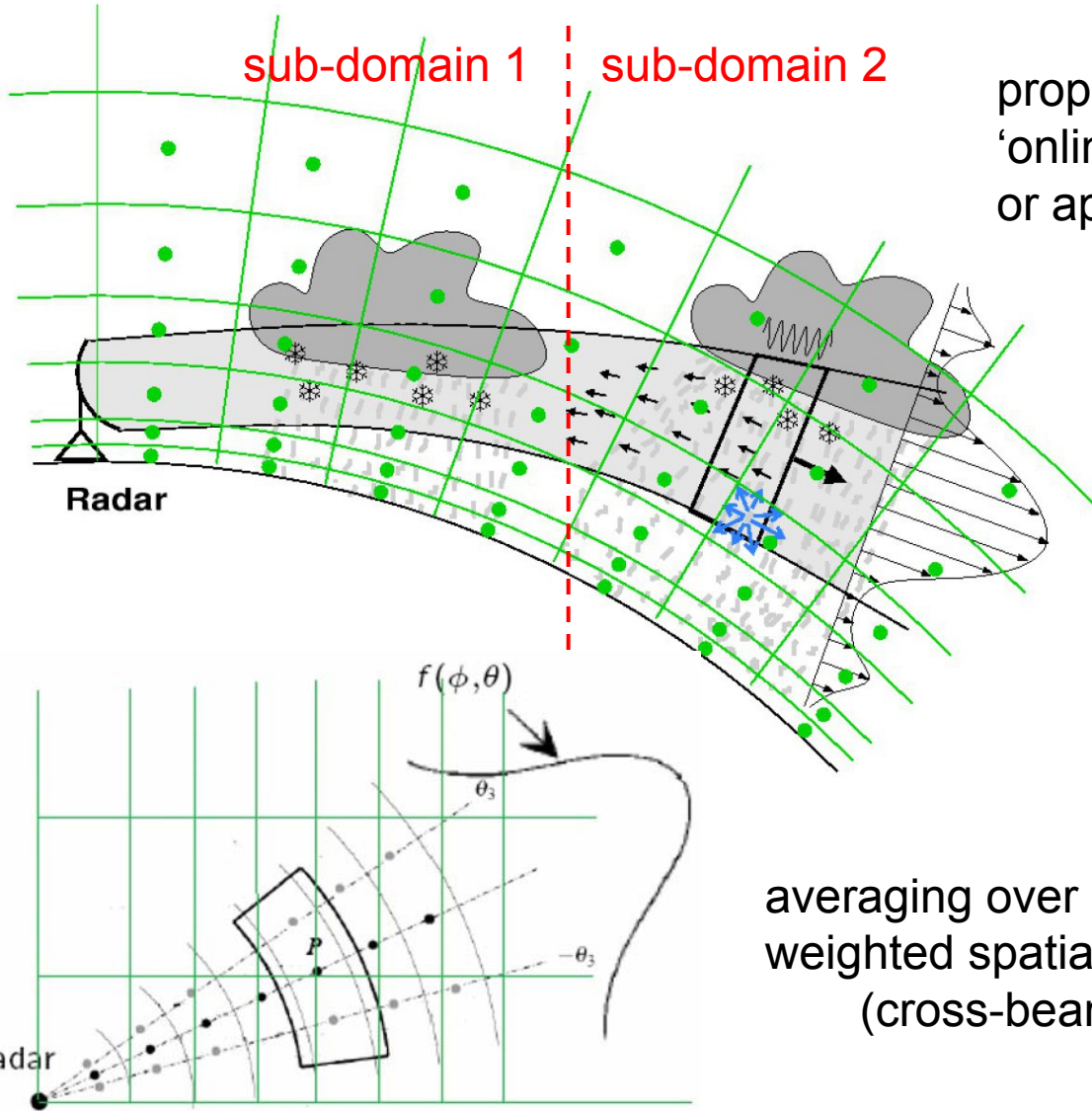
→ doing assimilation experiments : OSSE setup



# Radar Forward Operator



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propagation of radar beam :  
'online' depend. on refractive index,  
or approximate standard atmosphere

MPP parallelisation:  
beam in an azimuthal slice  
has to be collected on 1 PE

averaging over beam weighting function:  
weighted spatial mean over measuring volume  
(cross-beam vertically / horizontally)



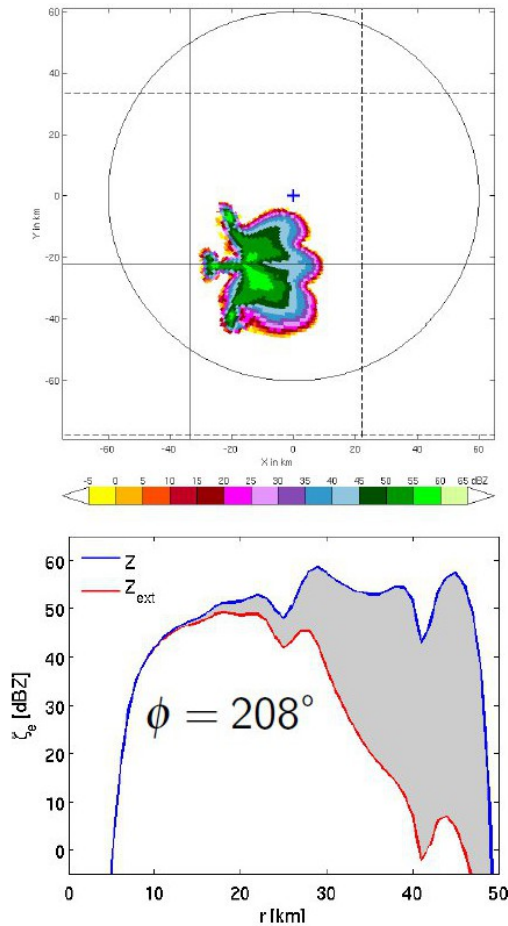
# Radar Forward Operator



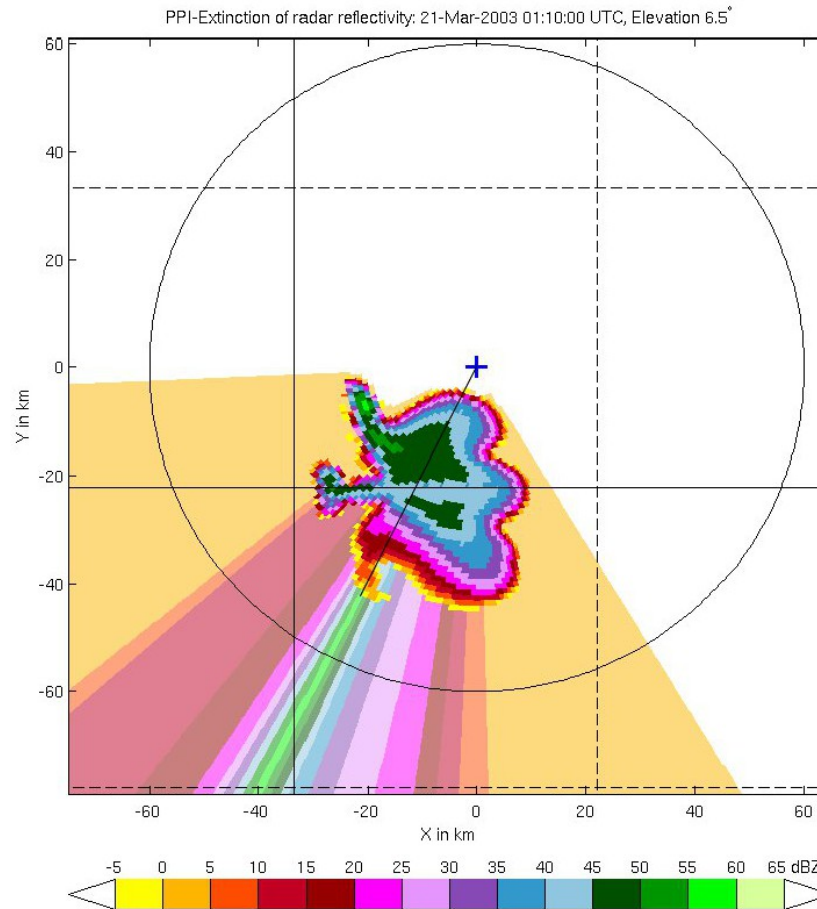
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without attenuation



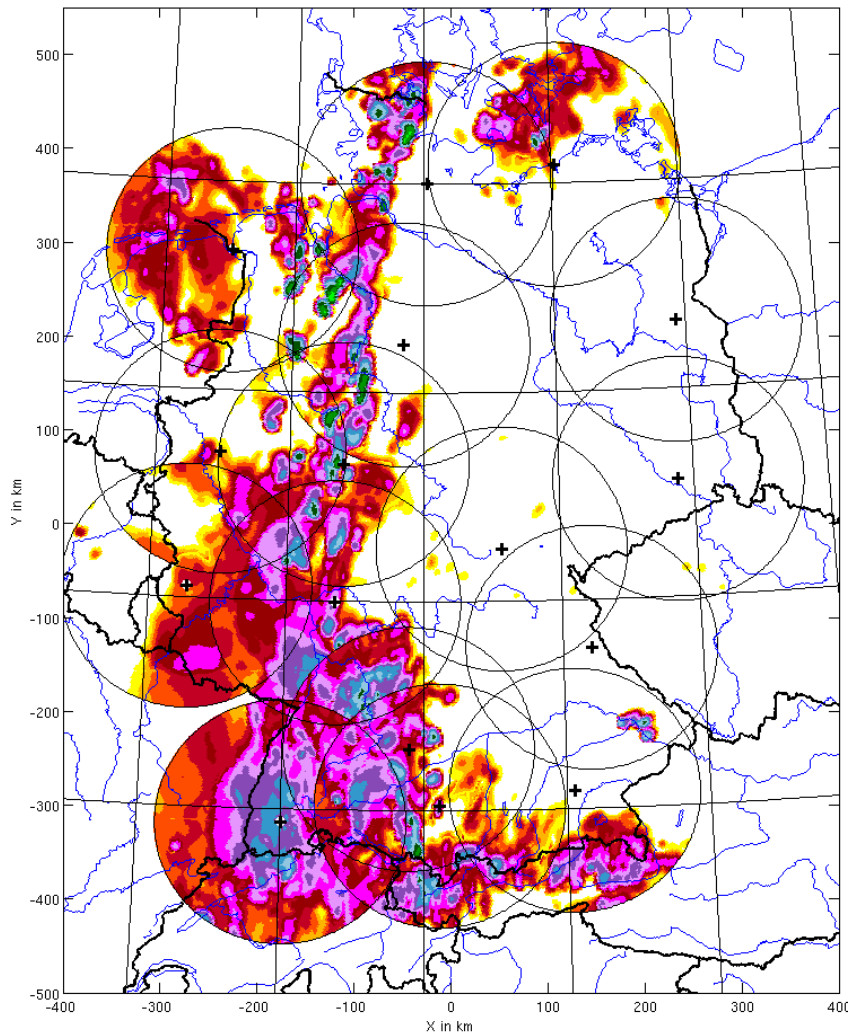
with attenuation of radar reflectivity  
by atmospheric gases + hydrometeors  
(using the extinction coefficients)



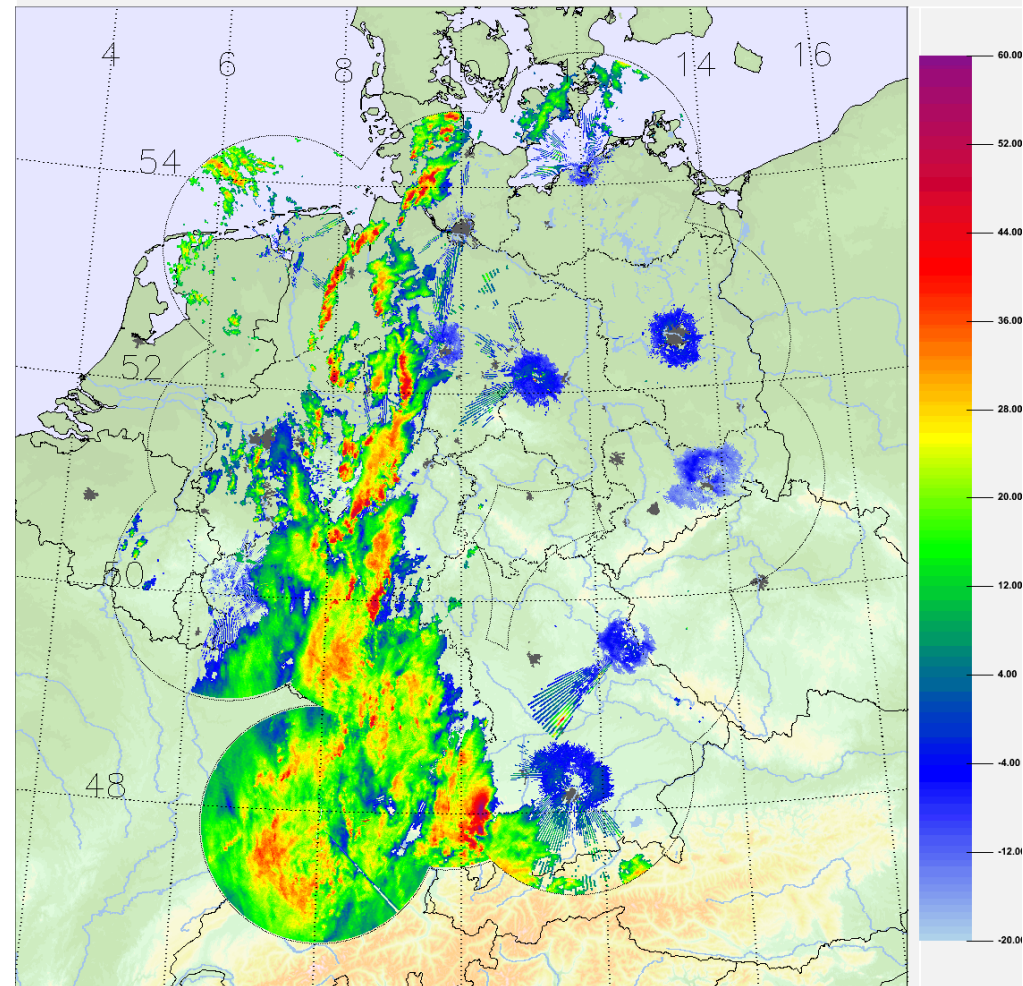


## Reflectivity of Operator against Observation

PPI-Z: All DWD Radars, 04-Sep-2011 15:30:00 UTC, Elevation 1.5°



20110904\_15-30-00: () ase,bin,drs,eis,emd,fbg,fld,ham,hann,muc,nhb,oft,ros,tur,umd



# Final slide...



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- Radar provide observation with high resolution in space and time
- Applicable for data assimilation, verification and process studies
- Careful quality check is necessary
- Assimilation of Radar data is applied in many NWP models
  - Radar wind were used in the first place but
  - Reflectivity is of increasing interest
  - Impact of the assimilation is still limited to the first forecast hours. Greatest benefit is achieved, when both variables are used.
  - further development is required
  - Issues: estimation of observation errors, thinning, superobbing...
  - some approaches try to use refractivity measurements





Thank you for your attention

Remarks?

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Questions?

