

HErZ Subproject 6: Ensemble methods - Representation of uncertainty in COSMO-DE-EPS

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Hans-Ertel-Zentrum für Wetterforschung
Deutscher Wetterdienst



⇒ Subproject goal: Improved representation of uncertainty in COSMO-DE-EPS

Main extensions planned:

- KENDA IC perturbations
- stochastic boundary layer parameterisation (under development at LMU)
- Focus of work so far: Analysis of the pre-operational COSMO-DE-EPS
 - EPS behaviour and impact(time) of different perturbations (in particular initial condition perturbations, ICPs)
 - dependence upon synoptic-scale forcing using the concept of the convective adjustment time scale

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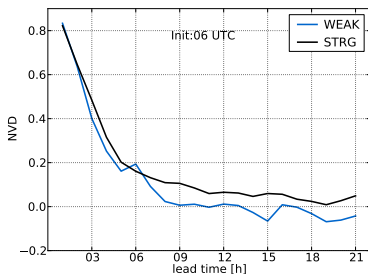
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Selected results:

- response of the EPS (bias und ensemble spread) very different under strong and weak forcing conditions
- impact of ICPs on ensemble variance and probabilistic forecast measures generally positive
- impact ICPs is generally largest in the first ~ 6 forecast hours and decays afterwards
- impact time of ICPs under strong forcing $\sim 9-21$ h, whereas under weak forcing $\sim 6-9$ h



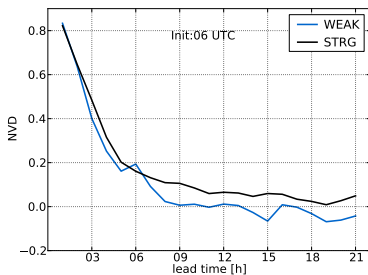
Normalised variance difference (Clark et al., 2009; Gebhardt et al., 2011):

$$NVD = \frac{\text{var}(P_{IBP}) - \text{var}(P_{BP})}{\text{var}(P_{IBP}) + \text{var}(P_{BP})}$$

- open question: structure of the ICPs (Meeting at the HErZ workshop in April 2012)

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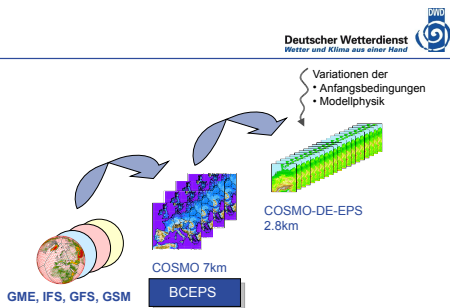
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Courtesy S. Theis

IC Perturbations (Peralta et al., JGR 2012):

$$f - f_0 = W(k)(f_{BC} - f_{EU})$$

f : Perturbed COSMO-DE-EPS prognostic fields ($u, v, T, q_v, [p']$); $\Delta_h = 2.8$ km

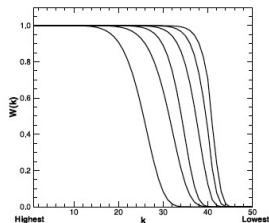
f_0 : COSMO-DE analysis ($\Delta_h = 2.8$ km)

f_{BC} : BCEPS ($\Delta_h = 7$ km)

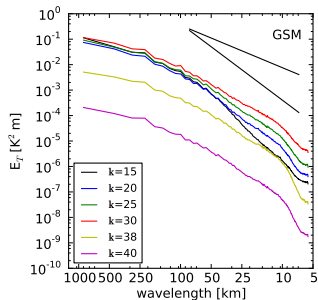
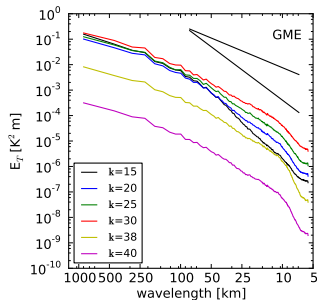
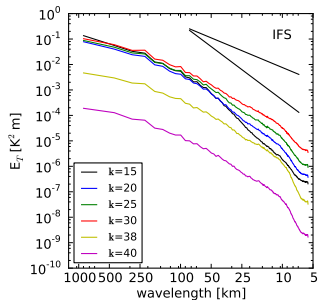
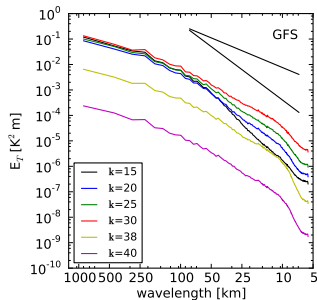
f_{EU} : COSMO-EU reference ($\Delta_h = 7$ km)

$W(k)$: filter at k th level

$$W(k) = \exp\left(-\epsilon \left|\frac{k}{N_{ke}}\right|^\gamma\right)$$

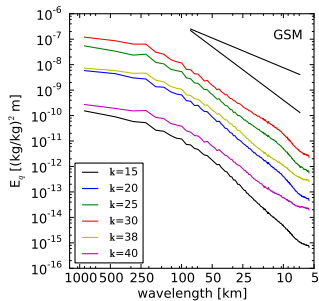
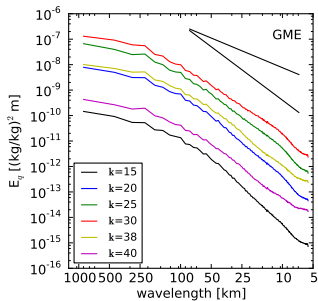
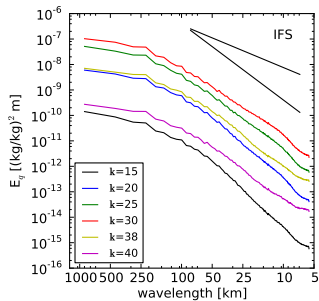
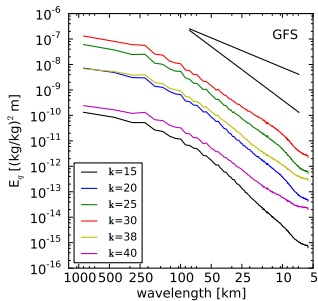


Spectra of temperature IC perturbations (May-Aug 2011, init: 06 UTC)



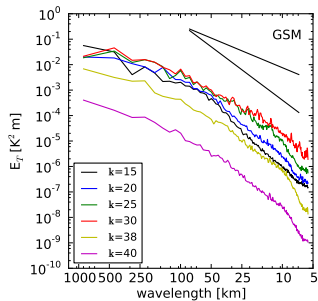
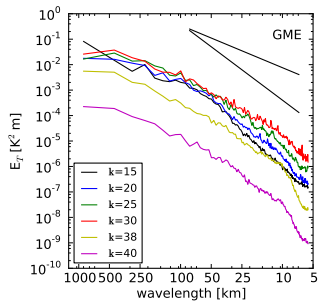
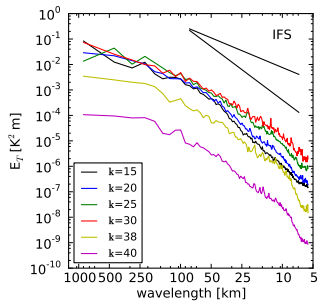
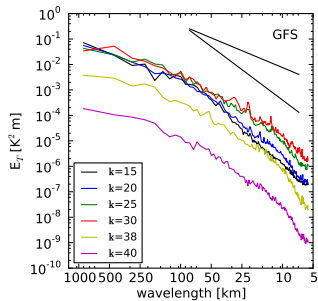
($k = 15, 20, 25, 30, 38, 40$ correspond to $\sim 10150, 7280, 4960, 3140, 1160, 830$ m altitude)

Spectra of specific humidity IC perturbations (May-Aug 2011, init: 06 UTC)



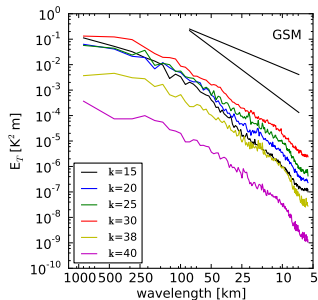
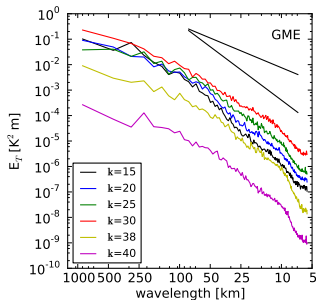
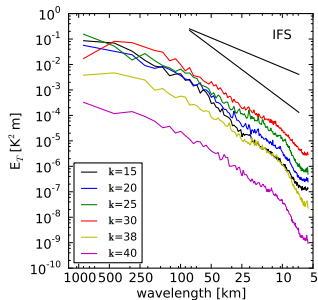
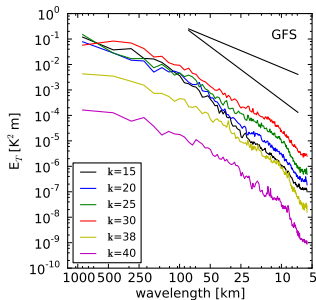
($k = 15, 20, 25, 30, 38, 40$ correspond to $\sim 10150, 7280, 4960, 3140, 1160, 830$ m altitude)

Spectra of temperature IC perturbations (Jun 5th 2011, init: 06 UTC)



($k = 15, 20, 25, 30, 38, 40$ correspond to $\sim 10150, 7280, 4960, 3140, 1160, 830$ m altitude)

Spectra of temperature IC perturbations (Jun 22nd 2011, init: 06 UTC)

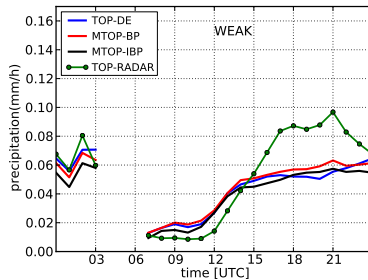
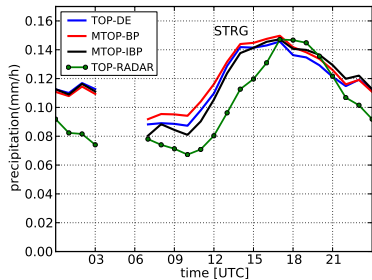


($k = 15, 20, 25, 30, 38, 40$ correspond to $\sim 10150, 7280, 4960, 3140, 1160, 830$ m altitude)

Next working steps:

- ◇ publication of results about regime-dependent impact of IC perturbations in COSMO-DE-EPS
- ◇ comparison study of structure and impact of analysed IC perturbations in current COSMO-DE-EPS with IC perturbations from COSMO-KENDA
 - test period for the comparison study ? June 2011 ?
 - setup for the comparison study ? KENDA-IC + BCEPS + PHY ?

Spatio-temporal mean of forecasted and observed precipitation



Mean and variance of IC perturbations (May-Aug 2011, init: 06 UTC)

| T | mean(GFS) | variance(GFS) | mean(GME) | variance(GME) | mean(GSM) | variance(GSM) |
|----------|----------------------|----------------------|----------------------|---------------------|----------------------|---------------------|
| $k = 15$ | $-3.9 \cdot 10^{-2}$ | $3.8 \cdot 10^{-1}$ | $1.9 \cdot 10^{-2}$ | $4.2 \cdot 10^{-1}$ | $-6.0 \cdot 10^{-4}$ | $3.6 \cdot 10^{-1}$ |
| $k = 20$ | $-1.8 \cdot 10^{-1}$ | $2.7 \cdot 10^{-1}$ | $9.5 \cdot 10^{-3}$ | $3.1 \cdot 10^{-1}$ | $-1.8 \cdot 10^{-1}$ | $2.5 \cdot 10^{-1}$ |
| $k = 25$ | $-1.1 \cdot 10^{-1}$ | $3.1 \cdot 10^{-1}$ | $-2.5 \cdot 10^{-2}$ | $3.6 \cdot 10^{-1}$ | $-2.6 \cdot 10^{-1}$ | $2.9 \cdot 10^{-1}$ |
| $k = 30$ | $-7.6 \cdot 10^{-2}$ | $4.0 \cdot 10^{-1}$ | $-3.2 \cdot 10^{-2}$ | $5.0 \cdot 10^{-1}$ | $-2.2 \cdot 10^{-1}$ | $3.8 \cdot 10^{-1}$ |
| $k = 38$ | $-6.4 \cdot 10^{-2}$ | $2.0 \cdot 10^{-2}$ | $-1.8 \cdot 10^{-2}$ | $2.4 \cdot 10^{-2}$ | $-6.4 \cdot 10^{-2}$ | $1.9 \cdot 10^{-2}$ |
| $k = 40$ | $-1.5 \cdot 10^{-2}$ | $7.6 \cdot 10^{-4}$ | $-3.5 \cdot 10^{-3}$ | $9.2 \cdot 10^{-4}$ | $-1.4 \cdot 10^{-2}$ | $7.4 \cdot 10^{-4}$ |
| $k = 44$ | $-2.3 \cdot 10^{-6}$ | $5.5 \cdot 10^{-10}$ | $-1.1 \cdot 10^{-9}$ | $4.6 \cdot 10^{-6}$ | $-2.3 \cdot 10^{-6}$ | 0.0 |

| q_v | mean(GFS) | variance(GFS) | mean(GME) | variance(GME) | mean(GSM) | variance(GSM) |
|----------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| $k = 15$ | $1.1 \cdot 10^{-6}$ | $4.7 \cdot 10^{-10}$ | $-3.4 \cdot 10^{-6}$ | $5.2 \cdot 10^{-10}$ | $1.1 \cdot 10^{-6}$ | $5.4 \cdot 10^{-10}$ |
| $k = 20$ | $-1.8 \cdot 10^{-5}$ | $2.5 \cdot 10^{-8}$ | $-1.8 \cdot 10^{-5}$ | $2.7 \cdot 10^{-8}$ | $-5.5 \cdot 10^{-1}$ | $2.4 \cdot 10^{-8}$ |
| $k = 25$ | $-8.2 \cdot 10^{-5}$ | $2.0 \cdot 10^{-7}$ | $-5.3 \cdot 10^{-5}$ | $2.2 \cdot 10^{-7}$ | $-1.3 \cdot 10^{-4}$ | $1.94 \cdot 10^{-7}$ |
| $k = 30$ | $-1.7 \cdot 10^{-4}$ | $4.5 \cdot 10^{-7}$ | $-9.2 \cdot 10^{-5}$ | $4.7 \cdot 10^{-7}$ | $-2.2 \cdot 10^{-4}$ | $4.8 \cdot 10^{-7}$ |
| $k = 38$ | $5.7 \cdot 10^{-6}$ | $2.9 \cdot 10^{-8}$ | $1.2 \cdot 10^{-6}$ | $3.9 \cdot 10^{-8}$ | $-2.6 \cdot 10^{-5}$ | $3.3 \cdot 10^{-8}$ |
| $k = 40$ | $2.7 \cdot 10^{-6}$ | $9.8 \cdot 10^{-10}$ | $7.1 \cdot 10^{-6}$ | $1.5 \cdot 10^{-9}$ | $-1.7 \cdot 10^{-2}$ | $1.1 \cdot 10^{-9}$ |
| $k = 44$ | $-4.7 \cdot 10^{-9}$ | $3.0 \cdot 10^{-13}$ | $6.1 \cdot 10^{-10}$ | $3.1 \cdot 10^{-13}$ | $-5.0 \cdot 10^{-9}$ | $3.0 \cdot 10^{-13}$ |

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Comparison of two EPS:

- (i) "IBP": pre-operational COSMO-DE-EPS with (IC+BC+PH) perturbations
 - (ii) "BP": special "Experiment 8247" in COSMO-DE-EPS with only (BC+PH) perturbations
-
- ◇ Both IBP and BP use 20 ensemble members
 - ◇ 3.5 month period from May 1st to August 15th 2011
 - ◇ 21 h-forecasts with initialisation times 00,06,12,18 UTC
 - ◇ Verification of total precipitation using DWD's high-resolution radar composite over Germany

- ◇ EPS performance in terms of convective precipitation forecasts under different meteorological conditions – strong vs. weak synoptic-scale forcing
- ◇ Convective adjustment time scale τ_c (Done et al. 2006; Zimmer et al. 2011; Keil and Craig 2011):

$$\tau_c = \frac{CAPE}{d(CAPE)/dt} = 0.5 \left(\frac{\rho_0 c_p T_0}{L_v g} \right) \frac{CAPE}{P}$$

- τ_c represents the rate at which convection releases conditional instability.
- τ_c small (e.g. < 6 h) indicates equilibrium convection (strong forcing)
- τ_c large (e.g. > 6 h) indicates non-equilibrium convection (weak forcing)

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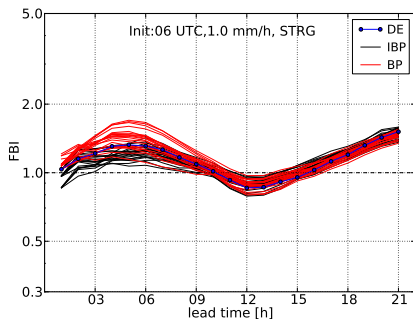
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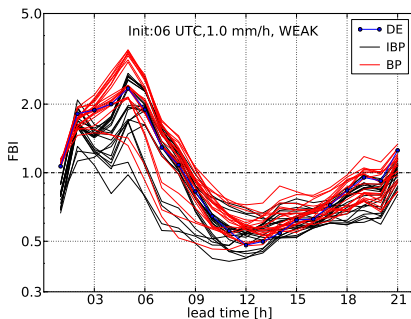
Forecast time series of frequency bias index (FBI); init 6 UTC

| | strong: $\langle \tau_c \rangle_{max} < 6 h$ | weak: $\langle \tau_c \rangle_{max} > 6 h$ | "dry" | missing | total |
|----------------|--|--|-------|---------|-------|
| number of days | 80 | 16 | 6 | 5 | 107 |

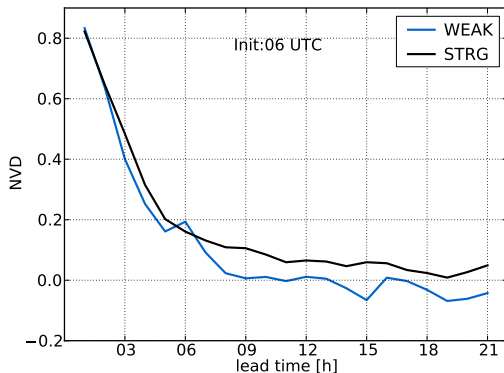
All days (80) with $\langle \tau_c \rangle_{max} < 6 h$



All days (16) with $\langle \tau_c \rangle_{max} > 6 h$



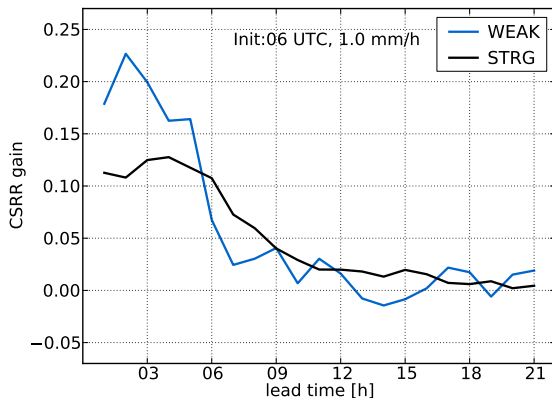
$$FBI = \frac{hits + false\ alarms}{hits + misses}$$



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Influence of initial condition perturbations on probabilistic measures



Single-threshold (1mm/h) conditional square-root of ranked probability score (Germann and Zawadzki, 2003; Kober et al., 2011):

$$\text{CSRR}(t) = \left(\frac{1}{|\Omega|} \int_{\Omega} [p(t_0 + t, \mathbf{x}) - \hat{p}(t_0 + t, \mathbf{x})]^2 d\mathbf{x} \right)^{0.5}$$

Consider CSRR gain:

$$\text{CSRRG} = 1 - \frac{\text{CSRR}_{\text{IBP}}}{\text{CSRR}_{\text{BP}}}$$